

# Chapter 5

# Geometry

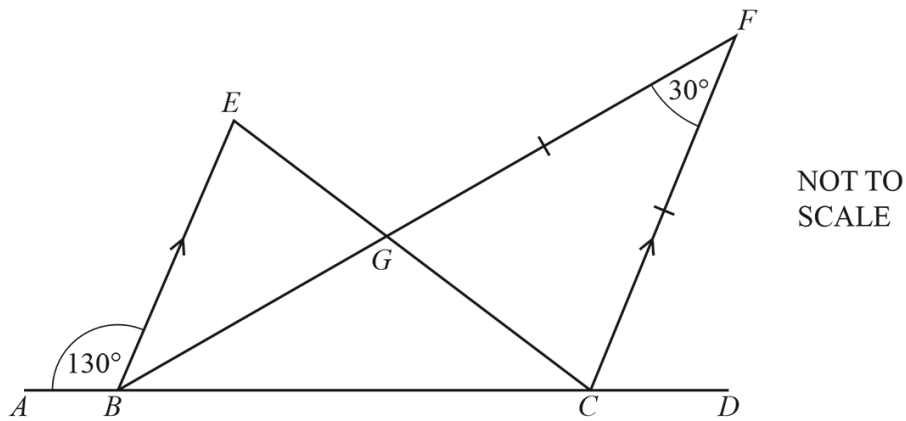


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01.0607\_m24\_qp\_42 Q: 7

(a)



$ABCD$  is a straight line and  $EC$  and  $BF$  meet at  $G$ .  
 $BE$  is parallel to  $CF$  and  $GF = CF$ .  
 Angle  $ABE = 130^\circ$  and angle  $BFC = 30^\circ$ .

Find

(i) angle  $FCD$

Angle  $FCD = \dots\dots\dots$  [2]

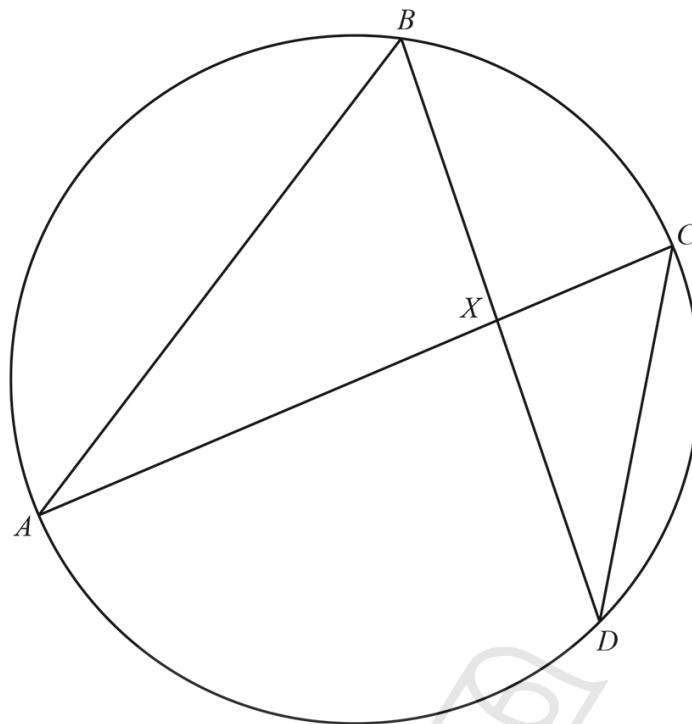
(ii) angle  $FBC$

Angle  $FBC = \dots\dots\dots$  [1]

(iii) angle  $BGE$ .

Angle  $BGE = \dots\dots\dots$  [2]

(b)



NOT TO  
SCALE

$A$ ,  $B$ ,  $C$  and  $D$  are points on the circle.  
 $AC$  and  $BD$  meet at  $X$ .

- (i) Show that triangles  $AXB$  and  $DXC$  are similar.  
Give a reason for each statement you make.

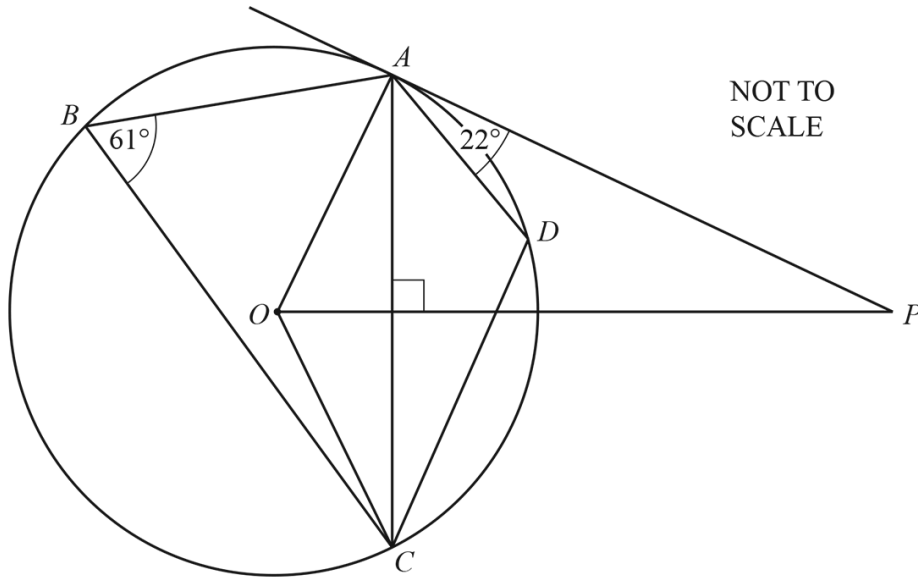
.....  
.....  
.....  
.....  
..... [2]

- (ii)  $AX = 5$  cm,  $XC = 2$  cm and  $XD = 4$  cm.

Find the length of  $BD$ .

$BD =$  ..... cm [3]

02. 0607\_s24\_qp\_41 Q: 5



NOT TO SCALE

$A, B, C$  and  $D$  lie on a circle, centre  $O$ .  
 $AP$  is a tangent to the circle at  $A$ .  
 $OP$  is perpendicular to  $AC$  and  $AD$  is parallel to  $BC$ .  
 Angle  $ABC = 61^\circ$  and angle  $PAD = 22^\circ$ .

(a) Write down the mathematical name of the cyclic quadrilateral  $ABCD$ .

..... [1]

(b) Complete the statement.

Angle  $OAP = 90^\circ$  because .....

..... [1]

(c) Find

(i) angle  $ADC$

Angle  $ADC =$  ..... [1]

(ii) angle  $ACD$

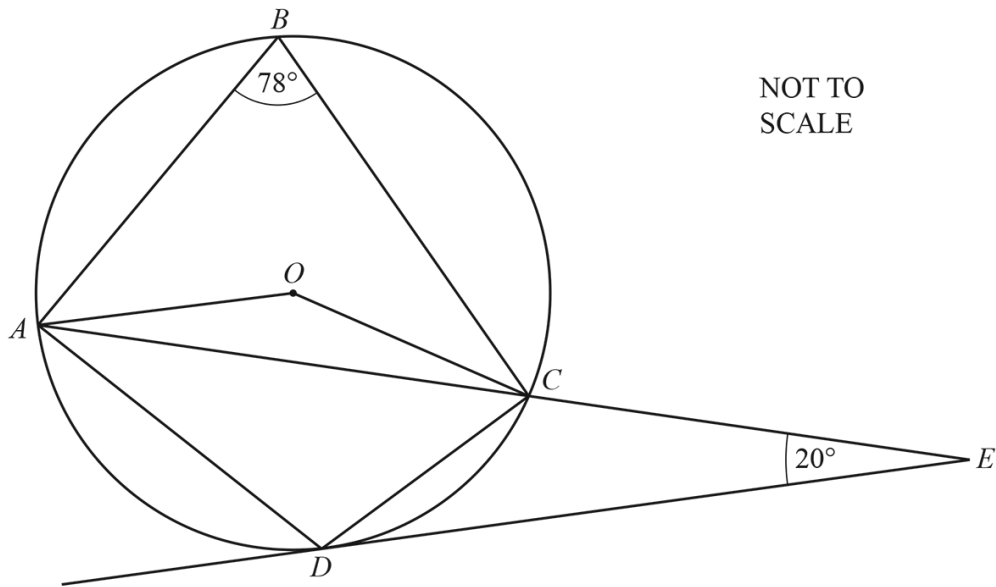
Angle  $ACD =$  ..... [1]

(iii) angle  $ACB$

Angle  $ACB =$  ..... [2]

(iv) angle  $OCA$ .

Angle  $OCA =$  ..... [2]



*A, B, C and D lie on a circle, centre O.  
 DE is a tangent to the circle at D.  
 ACE is a straight line.*

Find

(a) angle *AOC*

Angle *AOC* = ..... [1]

(b) angle *OAC*

Angle *OAC* = ..... [2]

(c) angle *ADC*

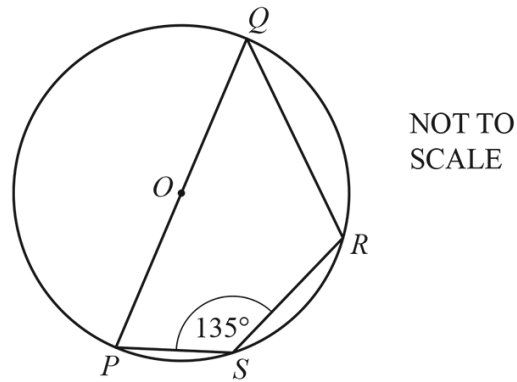
Angle *ADC* = ..... [1]

(d) angle *CAD*.

Angle *CAD* = ..... [3]

04. 0607\_w23\_qp\_42 Q: 10

(a)

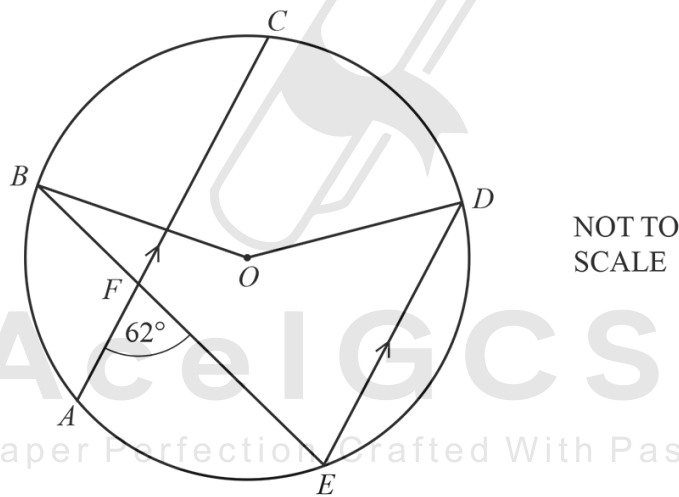


$P, Q, R$  and  $S$  are points on the circle centre  $O$ .

Find angle  $PQR$ .

Angle  $PQR = \dots\dots\dots$  [1]

(b)



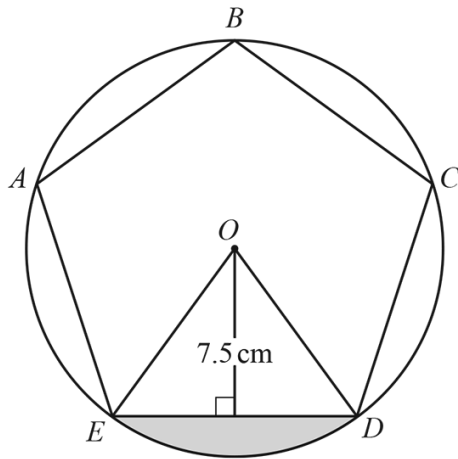
$A, B, C, D$  and  $E$  are points on the circle centre  $O$ .

$AC$  is parallel to  $ED$ .

Find the obtuse angle  $BOD$ .

Angle  $BOD = \dots\dots\dots$  [2]

(c)



NOT TO  
SCALE

$ABCDE$  is a regular pentagon.  
 $A, B, C, D$  and  $E$  are points on the circle centre  $O$ .  
The length of the perpendicular from  $O$  to  $ED$  is  $7.5$  cm.

(i) Show that the length of one side of the pentagon is  $10.9$  cm correct to 3 significant figures.

(ii) Calculate the shaded area.

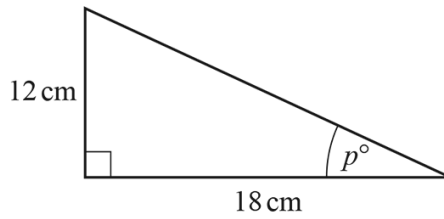
[4]

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.....  $\text{cm}^2$  [4]

05.0607\_w23\_qp\_43 Q: 11

(a)

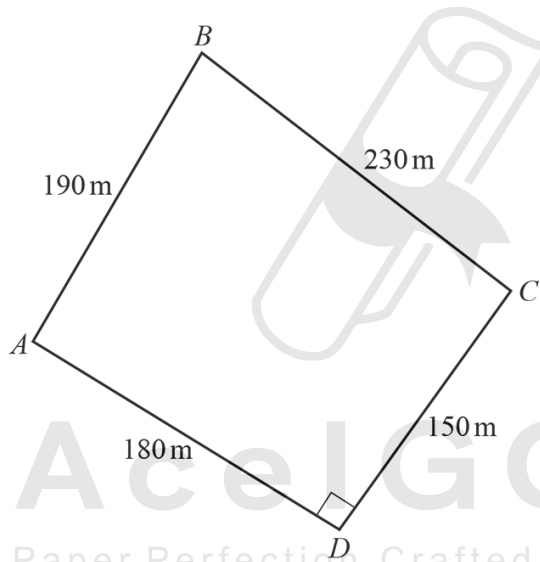


NOT TO SCALE

Calculate the value of  $p$ .

$p = \dots\dots\dots$  [2]

(b)



NOT TO SCALE

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(i) Show that angle  $ABC = 67.0^\circ$  correct to 1 decimal place.

[4]

(ii) Calculate the shortest distance from  $A$  to the side  $BC$ .

..... m [3]

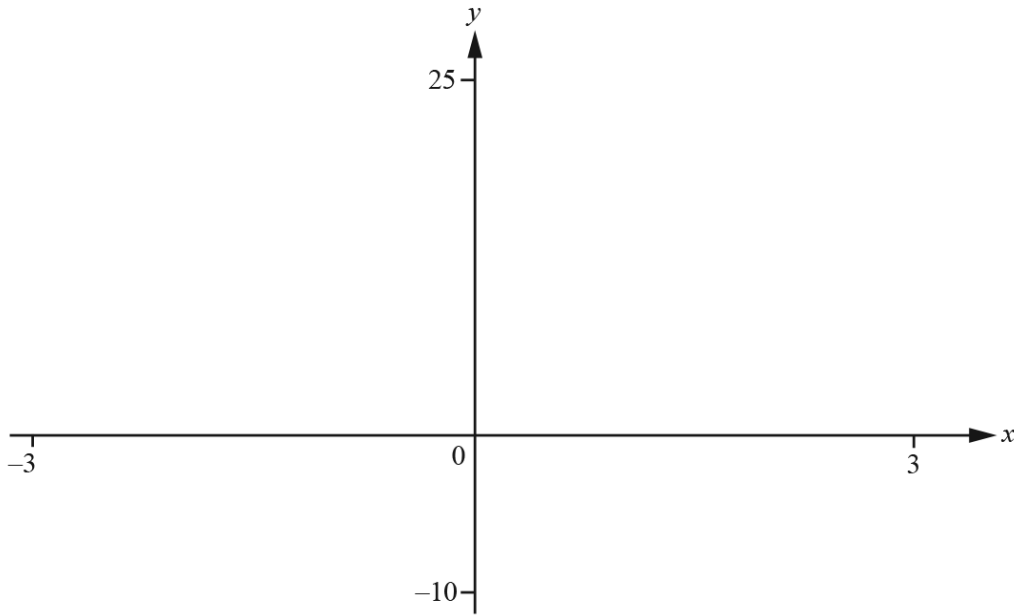
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06. 0607\_w16\_qp\_43 Q: 5



$$f(x) = x^3 - 4x + 6$$

(a) On the diagram, sketch the graph of  $y = f(x)$  for  $-3 \leq x \leq 3$ . [2]

(b) Solve the equation  $f(x) = 2x + 3$ .

$x = \dots\dots\dots$  or  $x = \dots\dots\dots$  or  $x = \dots\dots\dots$  [3]

(c) (i) Find the co-ordinates of the local maximum point and the local minimum point.

Maximum (....., .....) [3]

Minimum (....., .....) [3]

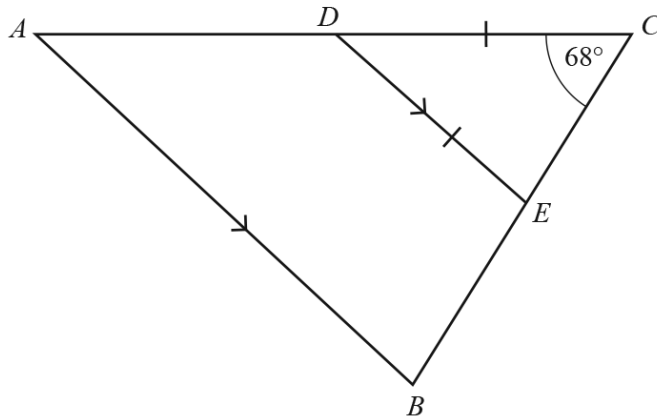
(ii) Find the range of values of  $k$  for which  $f(x) = k$  has only one solution.

..... [1]

(d) Describe fully the symmetry of the graph of  $y = f(x)$ .

.....  
 ..... [3]

(a)



NOT TO SCALE

In the diagram,  $ABC$  is a triangle and  $AB$  is parallel to  $DE$ .  
 Angle  $BCA = 68^\circ$  and  $DE = DC$ .

(i) Find angle  $BAC$ .

Angle  $BAC = \dots\dots\dots$  [2]

(ii) scalene      equilateral      isosceles      right-angled

Choose one word from the list to complete the statement.

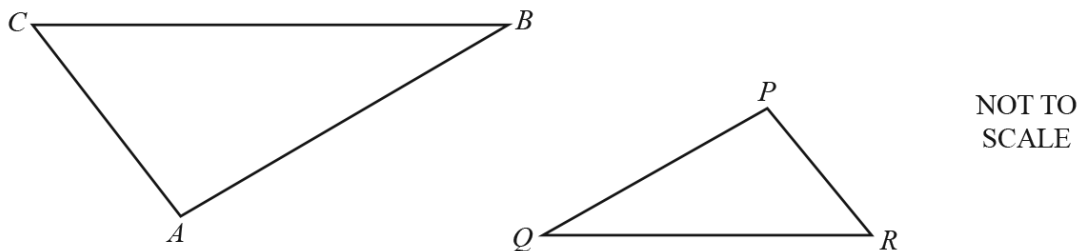
Triangle  $ABC$  is  $\dots\dots\dots$  [1]

(b) Calculate the interior angle of a regular 20 sided polygon.

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$\dots\dots\dots$  [3]

(c)



In the diagram, angle  $A =$  angle  $P$  and angle  $B =$  angle  $Q$ .

(i) Explain why angle  $C =$  angle  $R$ .

..... [1]

(ii)  $AB = 8$  cm,  $AC = 5$  cm,  $BC = 9$  cm and  $PR = 3$  cm.

(a) Complete the statement.

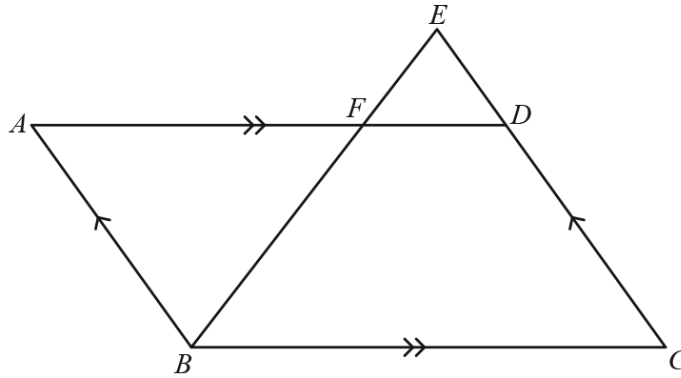
Triangle  $ABC$  is ..... to triangle  $PQR$  [1]

(b) Calculate  $QR$ .

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$QR =$  ..... cm [2]

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NOT TO SCALE

$ABCD$  is a parallelogram.  
 $BFE$  and  $CDE$  are straight lines.

- (a) Explain why triangles  $AFB$  and  $DFE$  are similar.

Answer(a) .....

.....

..... [2]

- (b)  $BC = 10$  cm,  $FD = 4$  cm and  $EC = 8$  cm.

- (i) Calculate the length of  $AB$ .

Answer(b)(i) ..... cm [3]

- (ii) Find the value of  $\frac{\text{Area of } DFE}{\text{Area of } AFB}$ .

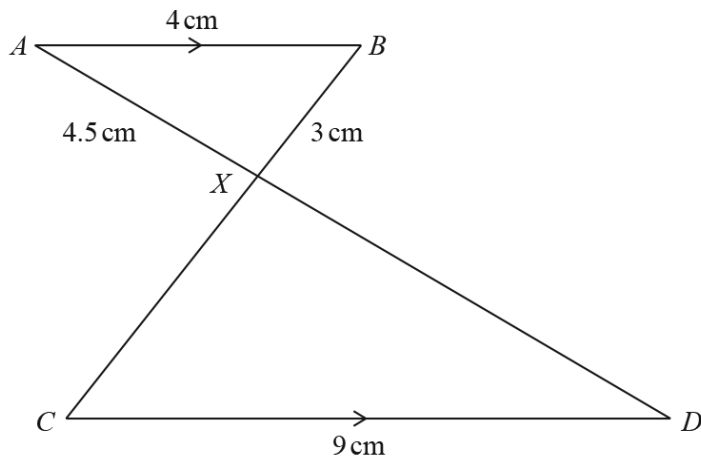
Answer(b)(ii) ..... [1]

- (iii) Find the value of  $\frac{\text{Area of } DFE}{\text{Area of } ABCD}$ .

Answer(b)(iii) ..... [2]

09. 0607\_w15\_qp\_41 Q: 4

(a)



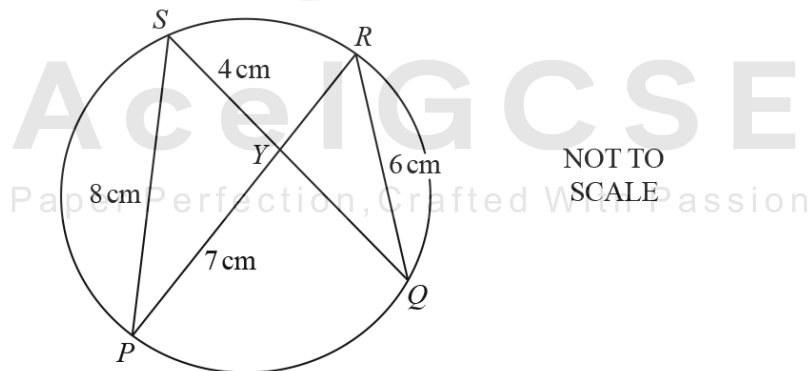
NOT TO SCALE

$AB$  and  $CD$  are parallel.  
 $AD$  and  $CB$  intersect at  $X$ .  
 $CD = 9\text{ cm}$ ,  $AB = 4\text{ cm}$ ,  $AX = 4.5\text{ cm}$  and  $BX = 3\text{ cm}$ .

Calculate the length of  $CX$ .

Answer(a) ..... cm [2]

(b)



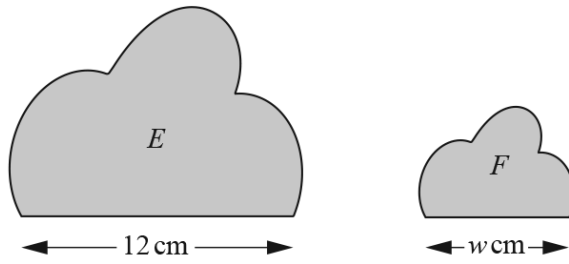
NOT TO SCALE

$P$ ,  $Q$ ,  $R$  and  $S$  lie on a circle.  
 $PR$  and  $QS$  intersect at  $Y$ .  
 $QR = 6\text{ cm}$ ,  $PS = 8\text{ cm}$ ,  $PY = 7\text{ cm}$  and  $YS = 4\text{ cm}$ .

Calculate the length of  $RY$ .

Answer(b) ..... cm [2]

(c)



NOT TO  
SCALE

The two shapes are mathematically similar.  
The area of  $E$  is  $90 \text{ cm}^2$  and the area of  $F$  is  $45 \text{ cm}^2$ .

Find the value of  $w$ .



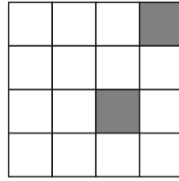
Answer(c)  $w = \dots\dots\dots$  [3]

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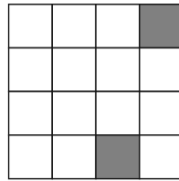
10. 0607\_w15\_qp\_43 Q: 4

- (a) (i) Shade in one more square so that the diagram has one line of symmetry.



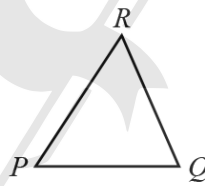
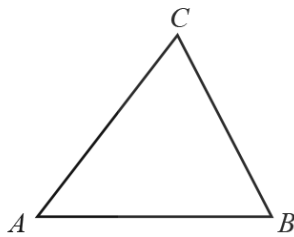
[1]

- (ii) Shade in two more squares so that the diagram has rotational symmetry of order 2 and no lines of symmetry.



[1]

(b)



NOT TO SCALE

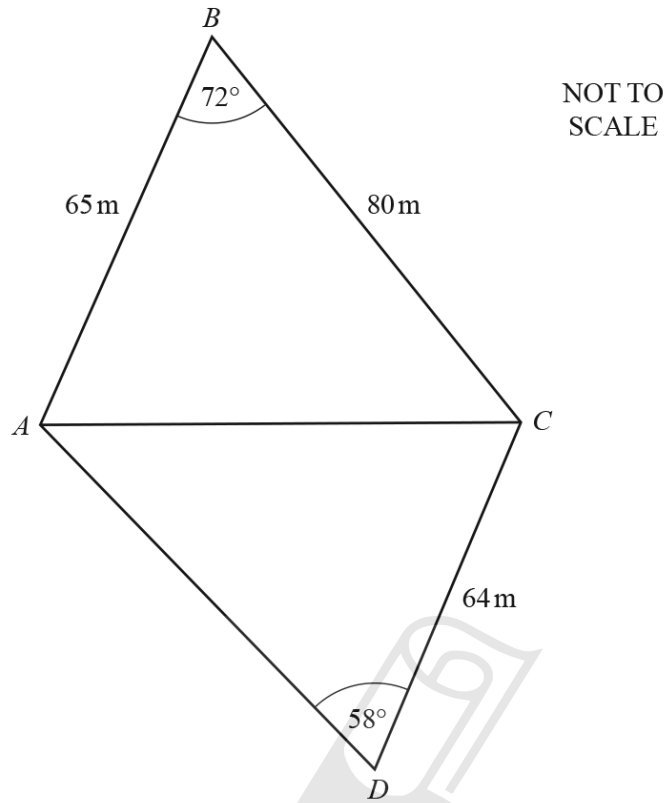
Triangle  $ABC$  and triangle  $PQR$  are mathematically similar.  
 $AB : PQ = 3 : 2$ .

- (i)  $CB = 10.5$  cm.  
 Calculate the length of  $RQ$ .

Answer(b)(i) ..... cm [2]

- (ii) The area of triangle  $ABC$  is  $45 \text{ cm}^2$ .  
 Calculate the area of triangle  $PQR$ .

Answer(b)(ii) .....  $\text{cm}^2$  [2]



(a) Find  $AC$ .

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Answer(a) ..... m [2]

(b) Calculate angle  $CAD$ .

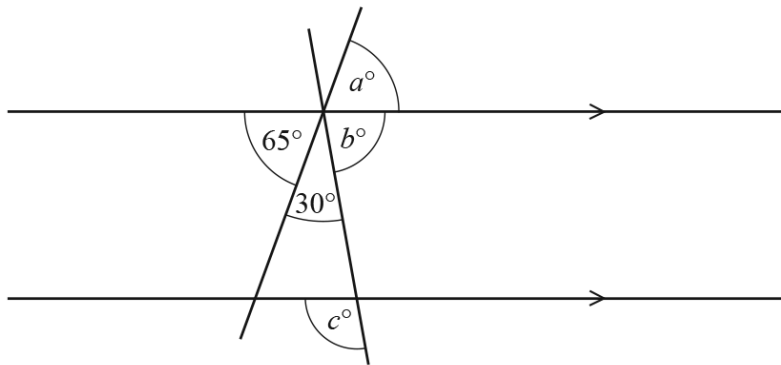
*Answer(b)* ..... [3]

(c) Calculate the area of the quadrilateral  $ABCD$ .

*Answer(c)* .....  $m^2$  [4]

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(a)



NOT TO SCALE

The diagram shows two straight lines crossing two parallel lines.

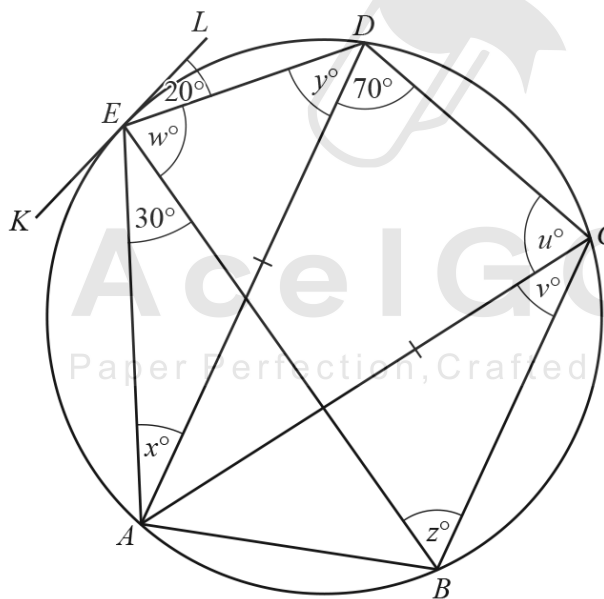
Find the values of  $a$ ,  $b$  and  $c$ .

$a = \dots\dots\dots$

$b = \dots\dots\dots$

$c = \dots\dots\dots$  [3]

(b)



NOT TO SCALE

$A, B, C, D$  and  $E$  are points on the circle.  
 $KL$  is a tangent to the circle at  $E$ .  
 $AC = AD$ .

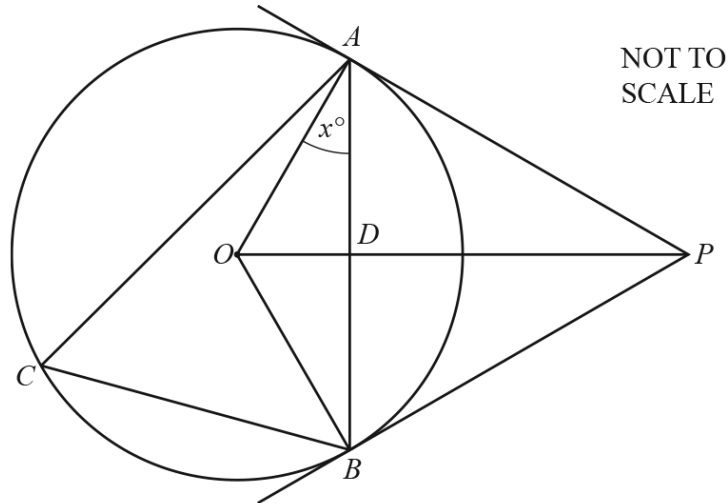
Find the values of  $u$ ,  $v$ ,  $w$ ,  $x$ ,  $y$  and  $z$ .

$u = \dots\dots\dots$        $x = \dots\dots\dots$

$v = \dots\dots\dots$        $y = \dots\dots\dots$

$w = \dots\dots\dots$        $z = \dots\dots\dots$  [6]

13. 0607\_w21\_qp\_43 Q: 9



$A, B$  and  $C$  lie on a circle, centre  $O$ .  
 $AP$  and  $BP$  are tangents to the circle.  
 $AB$  intersects  $OP$  at  $D$  and angle  $OAB = x^\circ$ .

(a) Write down the size of angle  $OBP$ .

Angle  $OBP = \dots\dots\dots$  [1]

(b) Find, in terms of  $x$ ,

(i) angle  $AOD$ ,

Angle  $AOD = \dots\dots\dots$  [1]

(ii) angle  $ACB$ ,

Angle  $ACB = \dots\dots\dots$  [1]

(iii) angle  $APB$ .

Angle  $APB = \dots\dots\dots$  [1]

(c) Write down the mathematical name of quadrilateral  $AOBP$ .

$\dots\dots\dots$  [1]

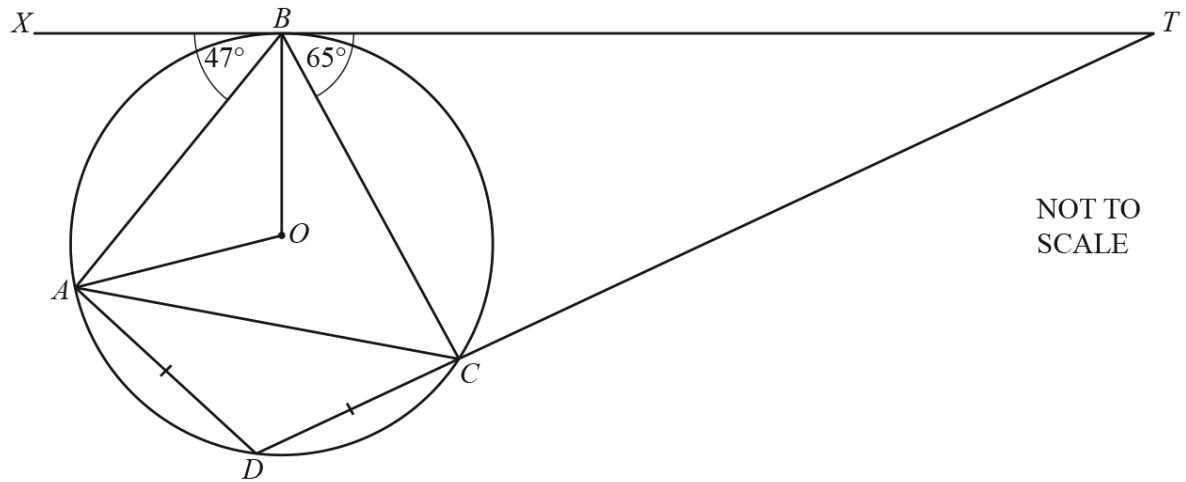
(d) Write down

(i) two triangles that are congruent,

$\dots\dots\dots$  [1]

(ii) two triangles that are similar but not congruent.

$\dots\dots\dots$  [1]



$A, B, C$  and  $D$  lie on a circle, centre  $O$ .  
 $AD = CD$  and  $XBT$  is a tangent to the circle at  $B$ .  
 $TCD$  is a straight line.  
 Angle  $XBA = 47^\circ$  and angle  $TBC = 65^\circ$ .

Find the value of

(a) angle  $OBX$ ,

Angle  $OBX = \dots\dots\dots$  [1]

(b) angle  $AOB$ ,

Angle  $AOB = \dots\dots\dots$  [2]

(c) angle  $CAO$ , Paper Perfection, Crafted With Passion

Angle  $CAO = \dots\dots\dots$  [2]

(d) angle  $CDA$ ,

Angle  $CDA$  = ..... [2]

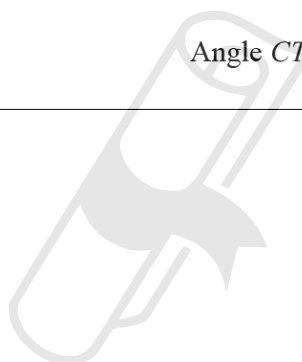
(e) angle  $DAC$ ,

Angle  $DAC$  = ..... [2]

(f) angle  $CTB$ .

Angle  $CTB$  = ..... [2]

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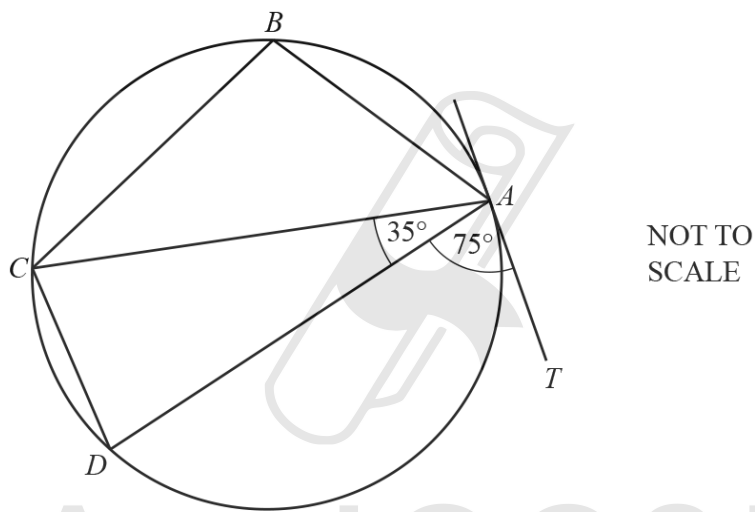
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15. 0607\_w20\_qp\_43 Q: 2

(a) Find the size of one interior angle of a regular polygon with 45 sides.

..... [3]

(b)



In the diagram,  $A$ ,  $B$ ,  $C$  and  $D$  lie on the circle.

$TA$  is a tangent to the circle at  $A$ .

Angle  $TAD = 75^\circ$  and angle  $DAC = 35^\circ$ .

Find

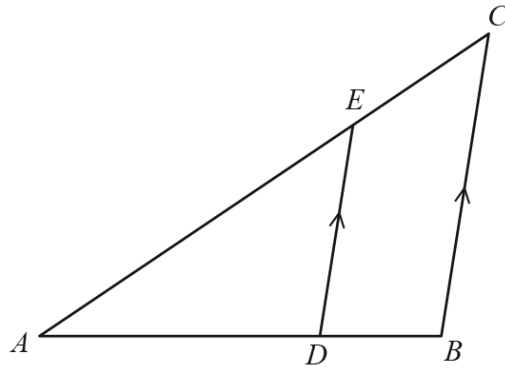
(i) angle  $ACD$ ,

Angle  $ACD = \dots\dots\dots$  [1]

(ii) angle  $ABC$ .

Angle  $ABC = \dots\dots\dots$  [2]

(c)



NOT TO SCALE

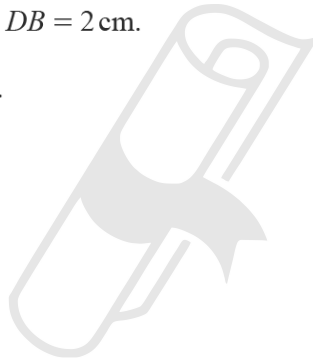
In the diagram,  $DE$  is parallel to  $BC$ .

(i) Complete the statement.

Triangle  $ADE$  is ..... to triangle  $ABC$ . [1]

(ii)  $AE = 6$  cm,  $EC = 3$  cm and  $DB = 2$  cm.

Calculate the length of  $AD$ .



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$AD =$  ..... cm [3]

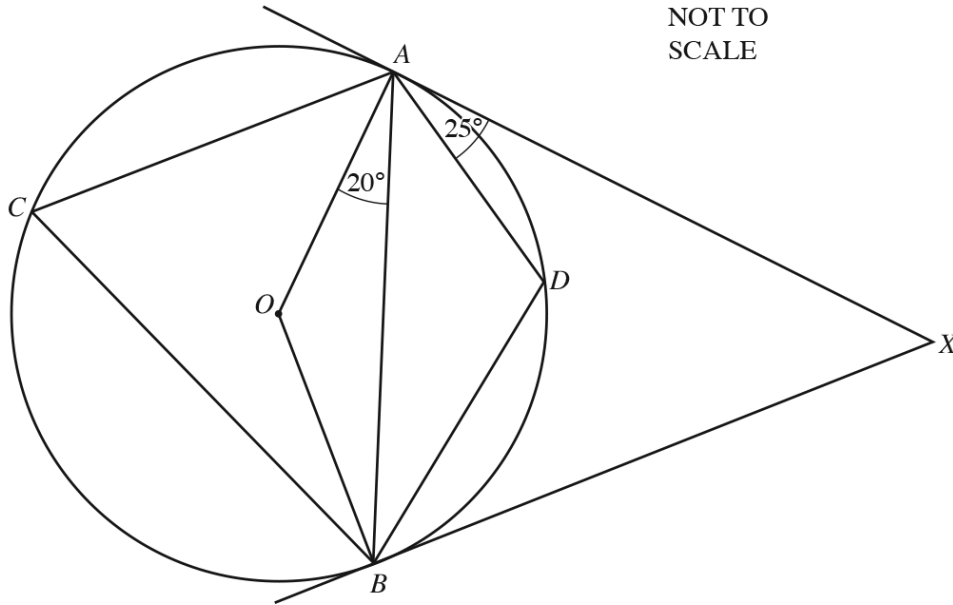
(iii) The area of triangle  $ADE$  is  $9 \text{ cm}^2$ .

Calculate the area of triangle  $ABC$ .

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.....  $\text{cm}^2$  [2]

NOT TO  
SCALE



$A$ ,  $B$ ,  $C$  and  $D$  lie on a circle, centre  $O$ .  
 $AX$  is a tangent to the circle at  $A$  and  $BX$  is a tangent to the circle at  $B$ .  
 Angle  $OAB = 20^\circ$  and angle  $DAX = 25^\circ$ .

(a) Find the value of

(i) angle  $AOB$ ,

Angle  $AOB = \dots\dots\dots$  [2]

(ii) angle  $ACB$ ,

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Angle  $ACB = \dots\dots\dots$  [1]

(iii) angle  $ADB$ ,

Angle  $ADB = \dots\dots\dots$  [1]

(iv) angle  $BAD$ ,

Angle  $BAD$  = ..... [1]

(v) angle  $DBA$ ,

Angle  $DBA$  = ..... [1]

(vi) angle  $AXB$ .

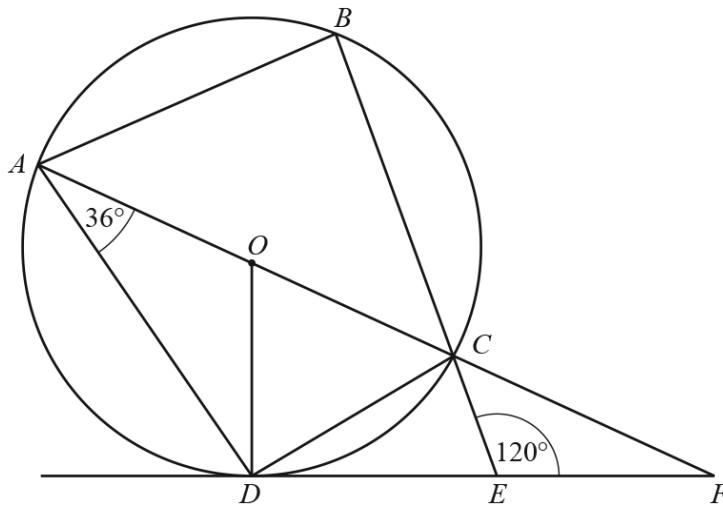
Angle  $AXB$  = ..... [1]

(b) What type of quadrilateral is  $ACBD$ ?

..... [1]



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NOT TO SCALE

*A, B, C and D lie on a circle, centre O.  
 DEF is a tangent to the circle at D.  
 AOCF and BCE are straight lines.*

**(a)** Complete the statement.

Angle  $ODE = 90^\circ$  because .....  
 ..... [1]

**(b)** Find the value of

**(i)** angle  $AOD$ ,

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 Paper Perfection, Crafted With Passion ..... [2]

**(ii)** angle  $ODC$ ,

Angle  $ODC =$  ..... [2]

(iii) angle  $ABC$ ,

Angle  $ABC = \dots\dots\dots$  [1]

(iv) angle  $CFD$ ,

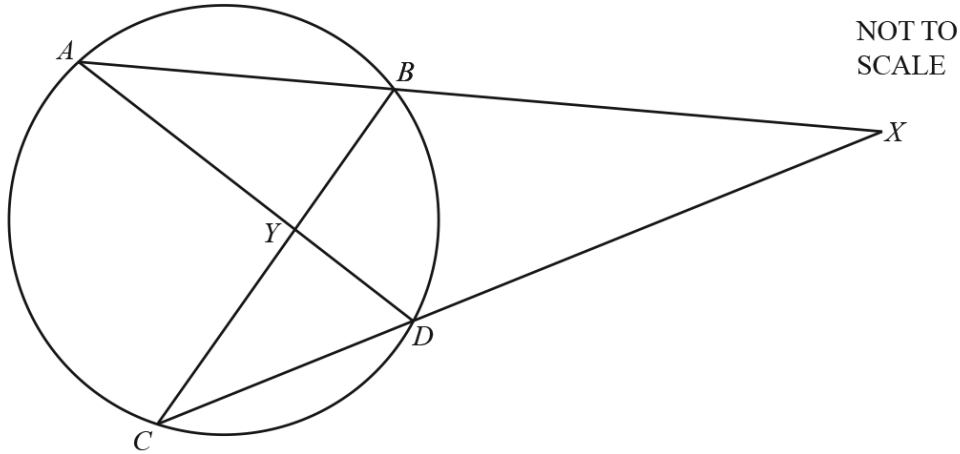
Angle  $CFD = \dots\dots\dots$  [1]

(v) angle  $CAB$ .

Angle  $CAB = \dots\dots\dots$  [1]

  
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$A, B, C$  and  $D$  are points on the circle.  
 $ABX, CDX, AYD$  and  $BYC$  are straight lines.

- (a) (i) Explain why triangle  $ADX$  is similar to triangle  $CBX$ .

.....  
 .....  
 ..... [2]

- (ii) Use part (a)(i) to show that  $XA \times XB = XC \times XD$

[1]

- (b)  $XB = 6$  cm,  $DC = 5$  cm and  $XD = 7$  cm.

Calculate the length  $AB$ .

..... cm [2]

- (c) Find the value of these fractions.

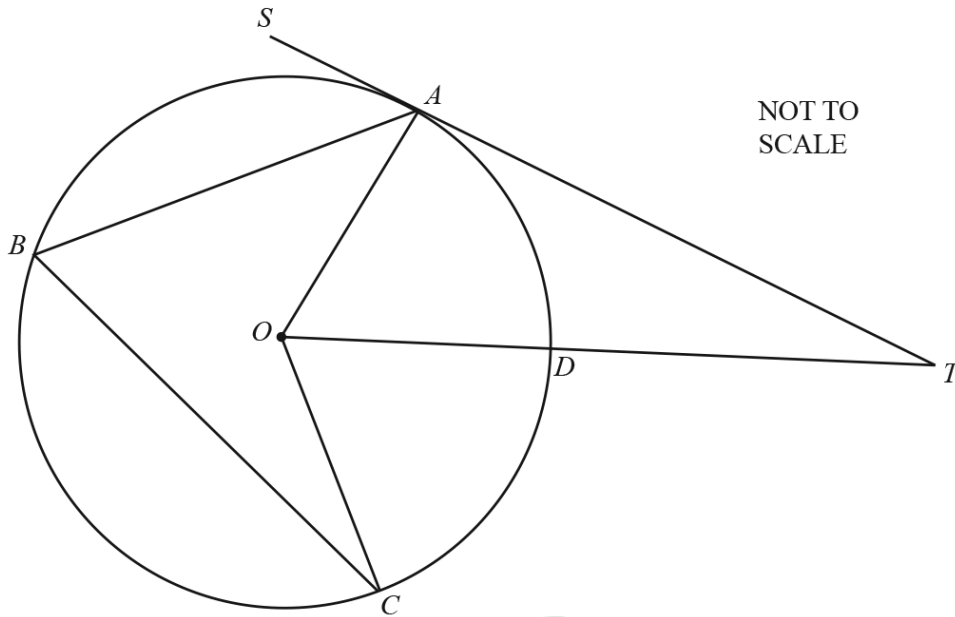
(i)  $\frac{\text{Area of triangle } ADX}{\text{Area of triangle } CBX}$

..... [1]

(ii)  $\frac{\text{Area of triangle } AYB}{\text{Area of triangle } CYD}$

..... [1]

19. 0607\_w18\_qp\_41 Q: 8



$A, B, C$  and  $D$  lie on a circle, centre  $O$ .  
 $ST$  is a tangent to the circle at  $A$ .  
 $ODT$  is a straight line that bisects angle  $AOC$ .

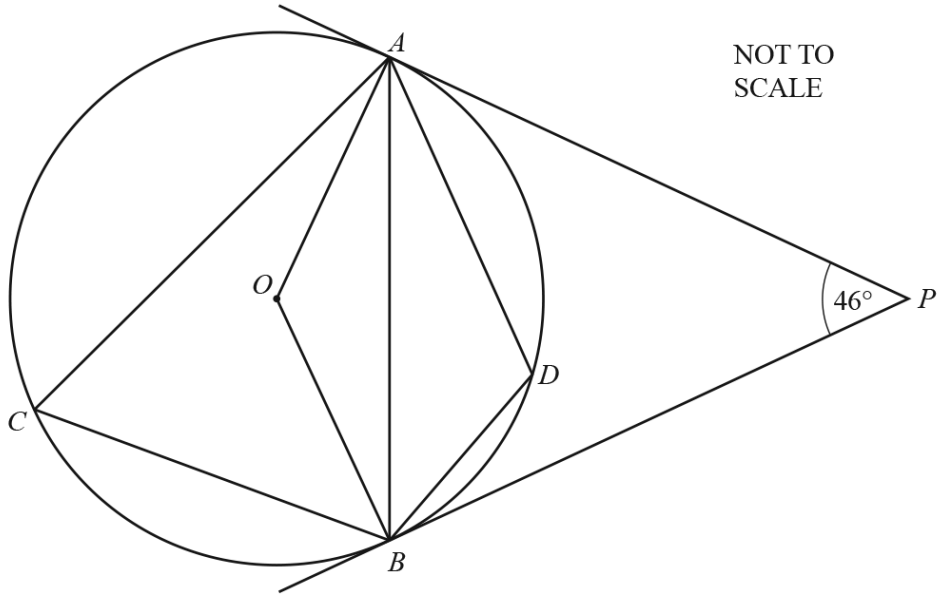
(a) Complete the statement.

Angle  $OAT = \dots\dots\dots$  because  $\dots\dots\dots$   
 $\dots\dots\dots$  [2]

(b)  $DT = OC$

Find angle  $ABC$ .

Angle  $ABC = \dots\dots\dots$  [4]



$A, B, C$  and  $D$  lie on a circle, centre  $O$ .  
 $AP$  and  $BP$  are tangents to the circle.  
 Angle  $APB = 46^\circ$ .

(a) Complete the statement.

Angle  $OAP = 90^\circ$  because .....  
 ..... [1]

(b) Find the value of

(i) angle  $AOB$ ,

Angle  $AOB = \dots\dots\dots$  [2]

(ii) angle  $OAB$ ,

Angle  $OAB = \dots\dots\dots$  [2]

(iii) angle  $ACB$ ,

Angle  $ACB = \dots\dots\dots$  [2]

(iv) angle  $ADB$ .

Angle  $ADB = \dots\dots\dots$  [2]

(c)  $OB$  bisects angle  $ABC$ .

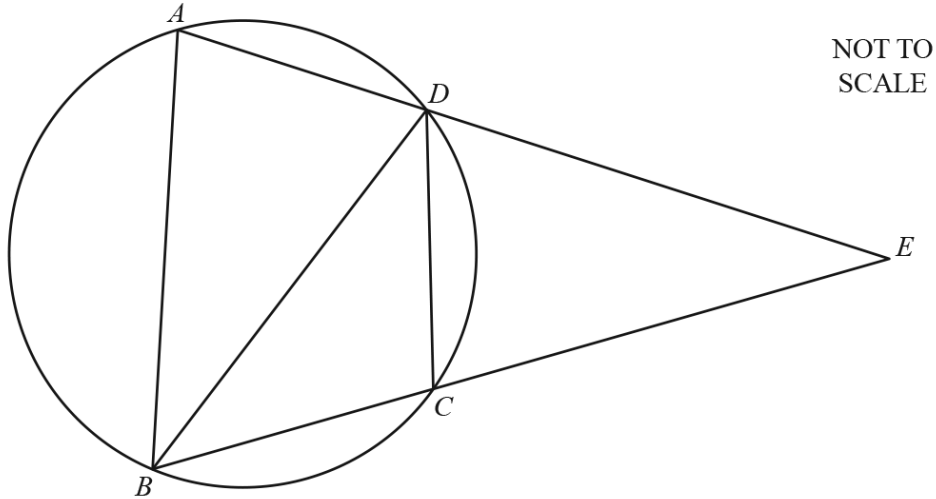
Find angle  $OAC$ .



Angle  $OAC = \dots\dots\dots$  [3]

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$A, B, C$  and  $D$  lie on a circle.  
 $ADE$  and  $BCE$  are straight lines that intersect at  $E$ .  
 $BD = DE$ , angle  $BAD = 4x$ , angle  $BCD = 6x$  and angle  $BDC = 3x$ .

Find

(a)  $x$ ,

$x = \dots\dots\dots$  [2]

(b) angle  $CBD$ ,

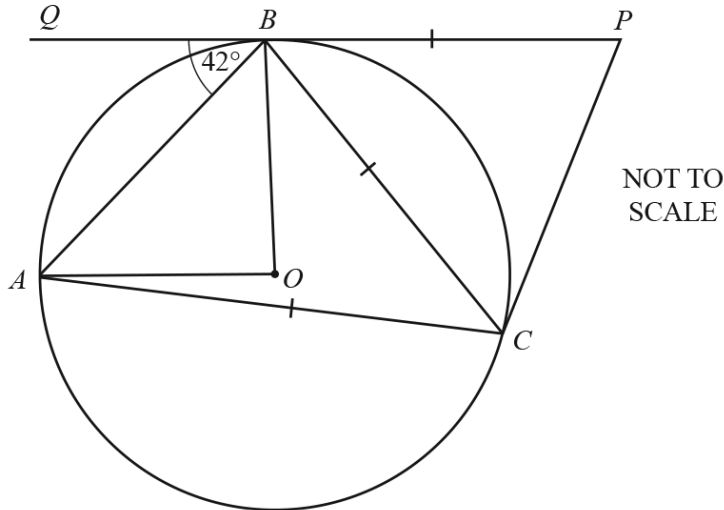


Angle  $CBD = \dots\dots\dots$  [2]

(c) angle  $CDE$ .

Angle  $CDE = \dots\dots\dots$  [3]

22. 0607\_w16\_qp\_42 Q: 4



$A$ ,  $B$  and  $C$  lie on a circle, centre  $O$ .  
 The line  $QBP$  is a tangent to the circle at  $B$ .  
 $AC = BC = BP$  and angle  $QBA = 42^\circ$ .

Find the value of

(a) angle  $OAB$ ,

Angle  $OAB = \dots\dots\dots [1]$

(b) angle  $AOB$ ,

Angle  $AOB = \dots\dots\dots [2]$

(c) angle  $BCA$ ,

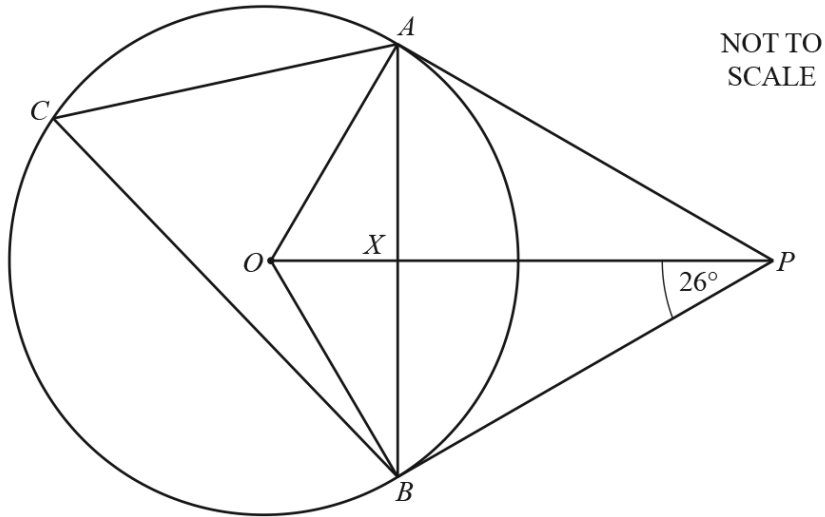
Angle  $BCA = \dots\dots\dots [1]$

(d) angle  $CBP$ ,

Angle  $CBP = \dots\dots\dots [2]$

(e) angle  $CPB$ .

Angle  $CPB = \dots\dots\dots [2]$



$A, B$  and  $C$  lie on a circle, centre  $O$ .  
 $AP$  and  $BP$  are tangents to the circle.  
 $AB$  intersects  $OP$  at the point  $X$  and angle  $OPB = 26^\circ$ .

(a) Find the size of

(i) angle  $ABP$ ,

Answer(a)(i) ..... [1]

(ii) angle  $OBA$ ,

Answer(a)(ii) ..... [1]

(iii) angle  $ACB$ .

Answer(a)(iii) ..... [1]

(b) Write down the mathematical name of quadrilateral  $AOBP$ .

Answer(b) ..... [1]

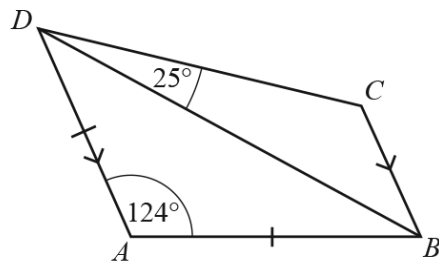
(c) Complete these statements.

(i) Triangle  $OBP$  is congruent to triangle ..... [1]

(ii) Triangle  $OBP$  is similar, but not congruent to, triangle ..... [1]

24. 0607\_w15\_qp\_43 Q: 9

(a)



NOT TO SCALE

In the quadrilateral  $ABCD$ ,  $DA = AB$  and  $DA$  is parallel to  $CB$ .  
 Angle  $DAB = 124^\circ$  and angle  $BDC = 25^\circ$ .

Calculate angle  $BCD$ .

*Answer(a)* ..... [3]

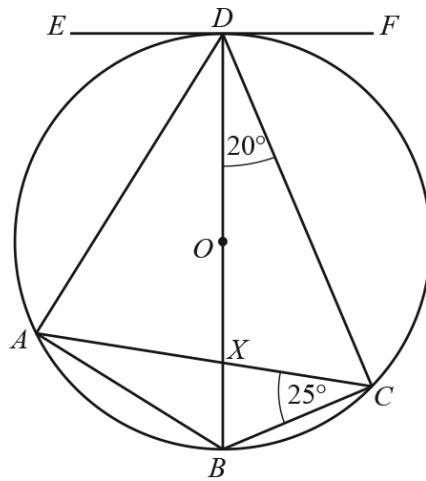
(b) Nine of the angles of a 10-sided polygon are each  $142^\circ$ .

Calculate the other angle.

*Answer(b)* ..... [3]

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(c)



NOT TO  
SCALE

$A, B, C$  and  $D$  lie on the circle, centre  $O$ .  
 $BD$  is a diameter and  $EDF$  is a tangent at  $D$ .  
 $AC$  and  $BD$  intersect at  $X$ .

Angle  $BCA = 25^\circ$  and angle  $BDC = 20^\circ$ .

Calculate

(i) angle  $ADE$ ,

Answer(c)(i) ..... [2]

(ii) angle  $DAC$ ,

Answer(c)(ii) ..... [2]

(iii) angle  $AXD$ .

Answer(c)(iii) ..... [1]



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01. 0607\_m24\_ms\_42 Q: 7

Question	Answer	Marks	Partial Marks
(a)(i)	50	2	<b>B1</b> for angle $BCF = 130$ or angle $EBC = 50$ soi by angle $EBG = 30$ and angle $GBC = 20$ or angle $FCG = 75$ and angle $GCB = 55$
(a)(ii)	20	1	

Question	Answer	Marks	Partial Marks
(a)(iii)	75	2	<b>M1</b> for $\frac{180-30}{2}$
(b)(i)	2 from Angle $AXB = \text{Angle } DXC$ [Vertically] opposite angles  Angle $ABX = \text{Angle } DCX$ Angles in same segment.  Angle $BAX = \text{Angle } CDX$ Angles in same segment.  And conclusion AA[A]	2	<b>B1</b> for 2 pairs correct with no/incorrect reasons and conclusion or for one pair correct with reason.
(b)(ii)	6.5	3	<b>B2</b> for $BX = 2.5$ or <b>M1</b> for $\frac{\dots}{2} = \frac{5}{4}$ oe

02. 0607\_s24\_ms\_41 Q: 5

Question	Answer	Marks	Partial Marks
(a)	trapezium	1	

Question	Answer	Marks	Partial Marks
(b)	Angle between tangent and radius oe	1	
(c)(i)	119	1	
(c)(ii)	22	1	
(c)(iii)	39	2	<b>M1</b> for $180 - \text{their (i)} - \text{their (ii)}$
(c)(iv)	29	2	<b>B1</b> for 61 or 122 at centre (may be on diagram)

03. 0607\_s23\_ms\_43 Q: 10

Question	Answer	Marks	Partial Marks
(a)	156	1	
(b)	12	2	M1 for $\frac{180 - \text{their}(a)}{2}$
(c)	102	1	
(d)	29	3	M2 for $x + x + \text{their}102 + 20 = 180$ oe or M1 for indicating angle $CDE =$ angle $DAC$

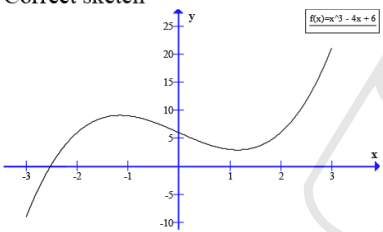
04. 0607\_w23\_ms\_42 Q: 10

Question	Answer	Marks	Partial Marks
(a)	45	1	
(b)	124	2	B1 for $BED = 62$
(c)(i)	$[EOD=] 72$ or $[ODE=] 54$	B1	seen or implied by 36
	$2 \times 7.5 \times \tan 36$ oe or $2 \times \frac{7.5}{\tan 54}$	M2	M1 for $\tan(36) = \frac{\text{halfside}}{7.5}$ or $\tan 54 = \frac{7.5}{\text{halfside}}$
	10.89....	A1	no errors or omissions
(c)(ii)	13.1 or 13.11 to 13.13...	4	M1 $r^2 = 7.5^2 + \left(\frac{10.9}{2}\right)^2$ or better or trig method for $r$ M1 $\frac{1}{2} \times 10.9 \times 7.5$ or $\frac{1}{2} \times \text{their } r^2 \times \text{their } \sin 72$ oe M1 $\frac{\text{their}72}{360} \times \pi \times \text{their } r^2$ oe

05. 0607\_w23\_ms\_43 Q: 11

Question	Answer	Marks	Partial Marks
(a)	33.7 or 33.69...	2	M1 for $\tan[p] = \frac{12}{18}$
(b)(i)	$150^2 + 180^2$	M1	
	$[\cos =] \frac{192^2 + 230^2 - \text{their}(180^2 + 150^2)}{2 \times 190 \times 230}$	M2	M1 for <i>their</i> $(180^2 + 150^2) = 190^2 + 230^2 - 2 \times 190 \times 230 \cos B$
	67.03 to 67.04	A1	
(b)(ii)	175 or 174.8 to 174.9...	3	M2 for $\sin 67[.0] = \frac{x}{190}$ oe or M1 for distance required is perpendicular to BC oe

06. 0607\_w16\_ms\_43 Q: 5

Question	Answer	Mark	Part Marks
(a)	Correct sketch 	2	B1 for correct cubic shape with maximum on left of minimum
(b)	-2.67 or -2.669 ... 0.524 or 0.5239 to 0.5240 2.15 or 2.145...	1 1 1	
(c) (i)	Maximum (-1.15, 9.08) Minimum (1.15, 2.92)	3	or (-1.155 to -1.154, 9.079...) or (1.154 to 1.155, 2.920 to 2.921) B2 for either maximum or minimum or B1 for 1 correct value
(ii)	$k < 2.92$ and $k > 9.08$	1FT	or above accuracy.
(d)	Rotational Order 2 (0, 6)	1 1 1	

07. 0607\_s17\_ms\_43 Q: 2

Question	Answer	Marks	Part Marks
(a)(i)	44	2	<b>M1</b> for [angle $BAC$ or $DEC$ =] $180 - 2 \times 68$ , soi by angle $CDE = 44$ or <b>M1</b> for angle $BAC = their$ angle $CDE$
(a)(ii)	isosceles	1	
(b)	162	3	<b>M2</b> for $180 - \frac{360}{20}$ or $\frac{180 \times (20 - 2)}{20}$ or <b>M1</b> for $\frac{360}{20}$ or $180 \times (20 - 2)$
(c)(i)	Angle sum of triangle oe	1	
(c)(ii)(a)	similar	1	
(c)(ii)(b)	5.4	2	<b>M1</b> for $\frac{5}{3} = \frac{9}{QR}$ oe



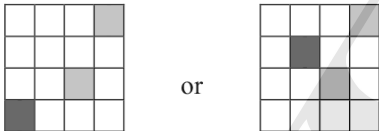
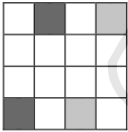
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Qu.	Answer	Mark	Part Marks
(a)	$ABF = DEF$ (alternate angles) $BAF = EDF$ (alternate angles) $AFB = DFE$ ([vert] opposite angles)	1 + 1	One mark for first fully correct and one for second fully correct.  or <b>B1</b> for any 2 pairs of angles <u>identified</u> without a reason or with an incorrect reason
(b) (i)	4.8 oe	3	<u>Method 1</u> Triangles $ABF, CEB$ [where $x = AB$ ] <b>M2</b> for $\frac{10}{6} = \frac{8}{x}$ oe or <b>M1</b> for $\frac{BC}{AF} = \frac{EC}{AB}$ oe  <u>Method 2</u> Triangles $ABF, DEF$ [where $x = AB$ ] <b>M2</b> for $\frac{8-x}{x} = \frac{4}{6}$ oe or <b>M1</b> for $\frac{FD}{AF} = \frac{ED}{AB}$ oe  <u>Method 3</u> Triangles $EFD, EBC$ [where $y = ED$ ] <b>M2</b> for $ED = 3.2$ or <b>M1</b> for $\frac{BC}{FD} = \frac{EC}{ED} \left[ = \frac{10}{4} = \frac{8}{y} \right]$ oe
(ii)	$\frac{4}{9}$ oe	1	
(iii)	$\frac{4}{30}$ oe	2	<b>M1</b> for Area of $ABF = \frac{3}{10}$ Area of $ABCD$ or ratio of $EFD$ to $EBC = 4 : 25$ oe soi or correct use of $\frac{1}{2}ab\sin C$ or e.g. $\frac{\frac{1}{2} \times theirED \times 4}{10 \times theirDC}$

09. 0607\_w15\_ms\_41 Q: 4

Question	Answer	Mark	Part Marks
(a)	6.75	2	M1 for $\frac{4}{9} = \frac{3}{CX}$ oe or better
(b)	3	2	M1 for $\frac{8}{6} = \frac{4}{RY}$ oe or better
(c)	8.49 or 8.484 to 8.485...	3	M2 for $\frac{12}{w} = \sqrt{\frac{90}{45}}$ oe or better or M1 for $\sqrt{\frac{90}{45}}$ or $\sqrt{\frac{45}{90}}$ oe soi or $\left(\frac{12}{w}\right)^2 = \frac{90}{45}$ oe

10. 0607\_w15\_ms\_43 Q: 4

Question	Answer	Mark	Part Marks
(a) (i)		1	
(ii)		1	
(b) (i)	7	2	M1 for $\frac{3}{2} = \frac{10.5}{RQ}$ oe or better
(ii)	20	2	M1 for $\left(\frac{3}{2}\right)^2$ or $\left(\frac{2}{3}\right)^2$ oe

11. 0607\_s15\_ms\_41 Q: 10

Qu.	Answer	Mark	Part Marks
(a)	86.1 or 86.08 to 86.09	2	M1 for $65^2 + 80^2 - 2 \times 65 \times 80 \times \cos 72$
(b)	39.1 or 39.07 to 39.09	3	M2FT for $[\sin A = ] \frac{64 \times \sin 58}{\text{their (a)}}$ or M1FT for $\frac{64}{\sin A} = \frac{\text{their } 86.1}{\sin 58}$ oe
(c)	5210 or 5206 to 5207	4FT	M1 for $0.5 \times 65 \times 80 \times \sin 72$ M2FT for $0.5 \times 64 \times \text{their } 86.1 \times \sin (180 - 58 - \text{their (b)})$ oe or M1 for $[\text{angle } ACD] = 180 - 58 - \text{their (b)}$

12. 0607\_m22\_ms\_42 Q: 4

Question	Answer	Marks	Partial Marks
(a)	[ a = ] 65 [ b = ] 85 [ c = ] 95	3	B1 for each
(b)	[ u = ] 70 [ v = ] 30 [ w = ] 80 [ x = ] 20 [ y = ] 50 [ z = ] 60	6	B1 for each  FT 180 – their u – their v  FT 150 – their x – their w FT 110 – their y

13. 0607\_w21\_ms\_43 Q: 9

Question	Answer	Marks	Partial Marks
(a)	90	1	
(b)(i)	$90 - x$ oe	1	
(b)(ii)	$90 - x$ oe	1	
(b)(iii)	$2x$	1	
(c)	Kite	1	
(d)(i)	<i>OAD</i> and <i>OBD</i> or <i>OAP</i> and <i>OBP</i> or <i>ADP</i> and <i>BDP</i>	1	

Question	Answer	Marks	Partial Marks
(d)(ii)	One from one of pairs in part (i) and One from one of other pairs in part (i)	1	

14. 0607\_w20\_ms\_41 Q: 5

Question	Answer	Marks	Partial Marks
(a)	90	1	
(b)	94	2	M1 for $180 - 43 - 43$ or $2 \times 47$

Question	Answer	Marks	Partial Marks
(c)	22	2	<b>B1</b> for $CAB = 65$ or $ACB = 47$
(d)	112	2	<b>M1</b> for $180 - \text{their } ABC$
(e)	34	2	<b>FT</b> <i>their</i> <b>(d)</b> <b>M1</b> for $(180 - \text{their}(\mathbf{d}))/2$
(f)	16	2	<b>B1</b> for $BCT = 99$

15. 0607\_w20\_ms\_43 Q: 2

Question	Answer	Marks	Partial Marks
(a)	172	3	<b>M2</b> for $180 - \frac{360}{45}$ or for $\frac{180 \times (45 - 2)}{45}$ or <b>M1</b> for $\frac{360}{45}$ (implied by 8) or for $180 \times (45 - 2)$ (implied by 7740)
(b)(i)	75	1	
(b)(ii)	110	2	<b>B1</b> for angle $CAT = 110$ or angle $CDA = 70$ or <b>M1</b> for $180 - \text{their angle } CDA$ .
(c)(i)	similar	1	
(c)(ii)	4	3	<b>M2</b> for $\frac{9}{6} = \frac{AD+2}{AD}$ oe or <b>M1</b> for $\frac{AD}{AB} = \frac{6}{9}$ oe
(c)(iii)	20.25	2	<b>M1</b> for $\left(\frac{3}{2}\right)^2$ or $\left(\frac{2}{3}\right)^2$ oe seen

16. 0607\_w19\_ms\_42 Q: 5

Question	Answer	Marks	Partial Marks
(a)(i)	140	2	<b>B1</b> for angle $OBA = 20$ soi
(a)(ii)	70	1	<b>FT</b> $0.5 \times \text{their}(\mathbf{i})$
(a)(iii)	110	1	<b>FT</b> $180 - \text{their}(\mathbf{ii})$

Question	Answer	Marks	Partial Marks
(a)(iv)	45	1	
(a)(v)	25	1	
(a)(vi)	40	1	
(b)	Cyclic [quadrilateral]	1	

17. 0607\_s18\_ms\_42 Q: 8

Question	Answer	Marks	Partial Marks
(a)	[Angle between] tangent and radius/diameter	1	
(b)(i)	108	2	M1 for $ADO = 36$ soi

Question	Answer	Marks	Partial Marks
(b)(ii)	54	2	M1 for $\frac{\text{their(b)(i)}}{2}$ or $90 - 36$ or $\frac{180 - 72}{2}$
(b)(iii)	90	1	
(b)(iv)	18	1	
(b)(v)	48	1	

18. 0607\_s18\_ms\_43 Q: 11

Question	Answer	Marks	Partial Marks
(a)(i)	Angle $X$ is common oe $\angle XCB = \angle XAD$ (angles in same segment) oe	2	B1 for each If 0 scored SC1 for 2 pairs of angles without reasons
(a)(ii)	$\frac{XA}{XC} = \frac{XD}{XB}$ oe	1	
(b)	8	2	M1 for $12 \times 7 = XA \times 6$ soi (implied by 14)
(c)(i)	$\frac{49}{36}$ oe	1	
(c)(ii)	$\frac{64}{25}$ oe	1	

19. 0607\_w18\_ms\_41 Q: 8

Question	Answer	Marks	Partial Marks
(a)	90 Angle [between] tangent and radius oe	2	B1 for each
(b)	60	4	B3 for angle $AOT = 60$ or M2 for $\sin(OAT) = \frac{1}{2}$ or $\cos(OAT) = \frac{1}{2}$ oe or M1 for $OT = 2OA$ oe

20. 0607\_s17\_ms\_41 Q: 5

Question	Answer	Marks	Partial Marks
(a)	[Angle between] tangent [and] radius / diameter [=90] oe	1	
(b)(i)	134	2	M1 for $360 - 90 - 90 - 46$ oe
(b)(ii)	23	2	M1 for $(180 - \text{their (i)}) \div 2$ oe
(b)(iii)	67	2	FT $(\text{their (i)}) \div 2$ M1 for $(\text{their (i)}) \div 2$ oe
(b)(iv)	113	2	FT $180 - \text{their (iii)}$ or $(360 - \text{their (i)}) \div 2$ M1 for $180 - \text{their (iii)}$ or $(360 - \text{their (i)}) \div 2$ oe
(c)	44	3	M2 for $180 - 67 - 23 - 23 - 23$ oe or $360 - 226 - 67 - 23$ oe or B1 for angle $OBC = 23$ or $226$ seen

21. 0607\_s16\_ms\_43 Q: 12

Question	Answer	Mark	Part Marks
(a)	18	2	M1 for $4x + 6x = 180$
(b)	18	2	M1 for $180 - 6x - 3x$
(c)	90	3	M2 for $180 - 3x - x - x$ or B1 for $CED = x$ or $DCE = 4x$

22. 0607\_w16\_ms\_42 Q: 4

Question	Answer	Mark	Part Marks
(a)	48	1	
(b)	84	2	FT $(180 - 2 \times \text{their (a)})$ , $\text{their (a)} \neq 45$ M1 for $(180 - 2 \times \text{their (a)})$ $\text{their (a)} \neq 45$
(c)	42	1	FT $\text{their (b)} \div 2$
(d)	69 cao	2	B1 for angle $OBC$ or $OAC = 21$ or angle $ABC = 69$
(e)	55.5	2	FT $\text{their (d)}$ M1 for $(180 - \text{their (d)}) \div 2$

23. 0607\_s15\_ms\_41 Q: 8

Qu.	Answer	Mark	Part Marks
(a) (i)	64	1	FT 90 – their (a)(i)
(ii)	26	1FT	
(iii)	64	1	
(b)	Kite or Cyclic Quadrilateral	1	
(c) (i)	<i>OAP</i>	1	
(ii)	<i>OXB</i> or <i>OXA</i>	1	

24. 0607\_w15\_ms\_43 Q: 9

Question	Answer	Mark	Part Marks
(a)	127	3	<b>M1</b> for angle $ADB$ or $ABD$ $= 0.5(180 - 124)$ implied by 28 in diagram <b>M1</b> for angle $DBC = \text{angle } ADB$ .
(b)	162	3	<b>M2</b> for $(10 - 2) \times 180 - 9 \times 142$ or <b>M1</b> for $(10 - 2) \times 180$
(c) (i)	65	2	<b>B1</b> for angle $ADB = 25$ or angle $ACD = 65$
(ii)	70	2	<b>B1</b> for angle $BAC = 20$ or angle $FDC = 70$
(iii)	85	1	

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