

Chapter 4

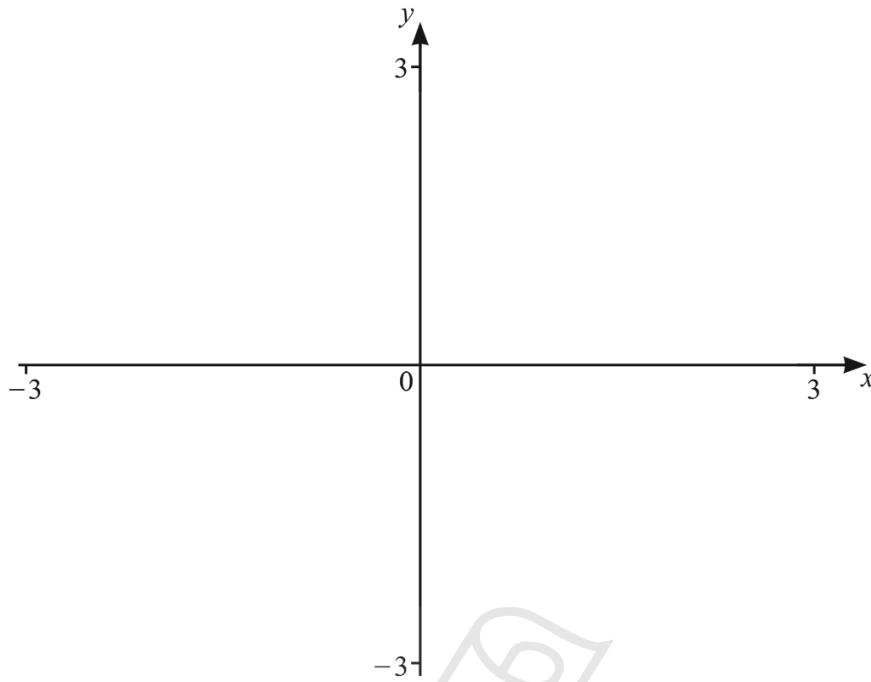
Coordinate geometry



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01. 0607_s24_qp_41 Q: 6



$$f(x) = 2 - |1 - 0.5x^2|$$

- (a) On the diagram, sketch the graph of $y = f(x)$, for values of x between -3 and 3 . [3]
- (b) The graph cuts the x -axis at points A and B .

Work out the length AB .

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$AB = \dots\dots\dots$ [2]

- (c) Solve $f(x) = 0.5$.
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 [2]

- (d) Write down the coordinates of the minimum point of the graph.
 (.....,) [1]

- (e) The equation $f(x) = k$ has two solutions.
 Find the range of values of k .
 [2]

02. 0607_s24_qp_43 Q: 4

Line L has equation $3y + 2x = 8$.

(a) Find the gradient and the y -intercept of line L .

gradient

y -intercept [3]

(b) Line P passes through the point $(2, 10)$ and is perpendicular to line L .

Show that the equation of line P is $2y - 3x = 14$.



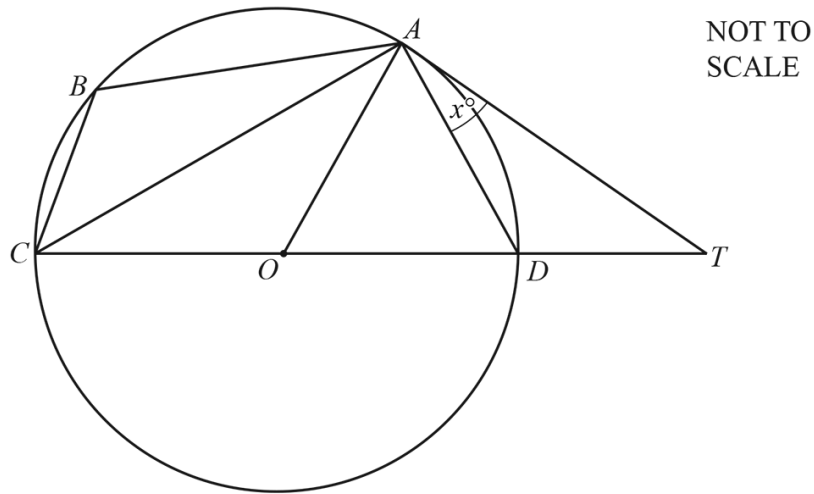
[3]

(c) Find the coordinates of the point where line L and line P intersect.
You must show all your working.

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(.....,) [4]

03. 0607_m23_qp_42 Q: 3



A, B, C and D lie on a circle, centre O .
 $CODT$ is a straight line.
 AT is a tangent to the circle at A .
 Angle $DAT = x^\circ$.

(a) Complete the statement.

Angle $CAD = 90^\circ$ because

..... [1]

(b) Find, in terms of x ,

(i) angle ACD

Angle $ACD =$ [1]

(ii) angle AOD

Angle $AOD =$ [1]

(iii) angle AOC

Angle $AOC =$ [1]

(iv) angle ADO

Angle $ADO =$ [1]

(v) angle ABC .

Angle $ABC =$ [1]

(c) Given that angle $DTA = y^\circ$, find y in terms of x .

$y =$ [1]

04. 0607_s23_qp_41 Q: 5

(a) The equation of line L is $y = 4x + 7$.

(i) Write down the gradient of line L .

..... [1]

(ii) Write down the coordinates of the point where line L cuts the y -axis.

(.....,) [1]

(b) A is the point $(3, 1)$ and B is the point $(11, 5)$.

(i) Calculate the length of AB .

..... [3]

(ii) Find the equation of the perpendicular bisector of the line AB .
Give your answer in the form $y = mx + c$.

$y =$ [5]

05.0607_w23_qp_43 Q: 12

(a) Find the coordinates of the point where the line $y = 3x + 7$ crosses

(i) the y -axis

(.....,) [1]

(ii) the line $y = 2$.

(.....,) [2]

(b) A is the point $(-5, 8)$ and B is the point $(1, -2)$.

Find the equation of the perpendicular bisector of AB .



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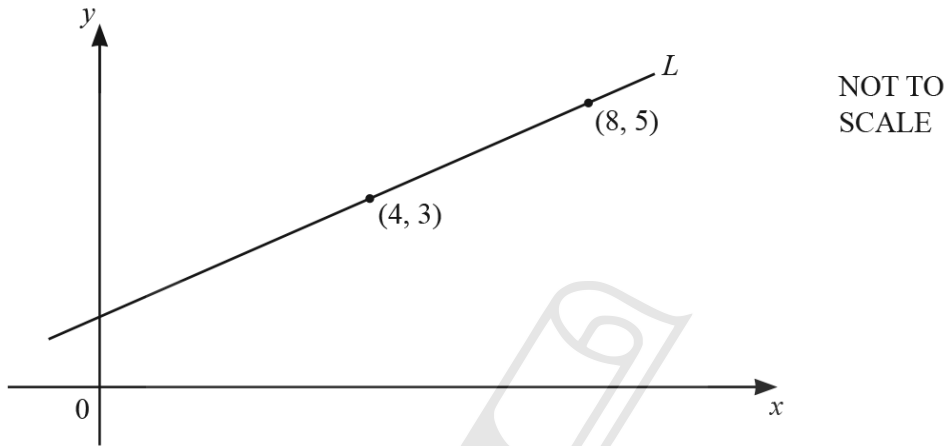
..... [5]

(a) Find the gradient and y -intercept of the line with equation $3x + 4y = 24$.

Gradient =

y -intercept = [3]

(b)



The diagram shows line L and the coordinates of two points on the line.

(i) Show that the equation of line L is $2y - x = 2$.



[3]

(ii) Find the equation of the line parallel to L that passes through the point $(0, 7)$.
Give your answer in the form $y = mx + c$.

$y =$ [2]

07. 0607_m21_qp_42 Q: 3

(a) (i) Write down the coordinates of the point where the line $y = -2x + 3$ crosses the y -axis.

(.....,) [1]

(ii) Write down the gradient of the line $y = -2x + 3$.

..... [1]

(b) The line $x + y = 6$ crosses the line $x = -2$ at point A .

Find the y -coordinate of A .

..... [1]

(c) Find the equation of the straight line that passes through the points $(3, -1)$ and $(12, 5)$.



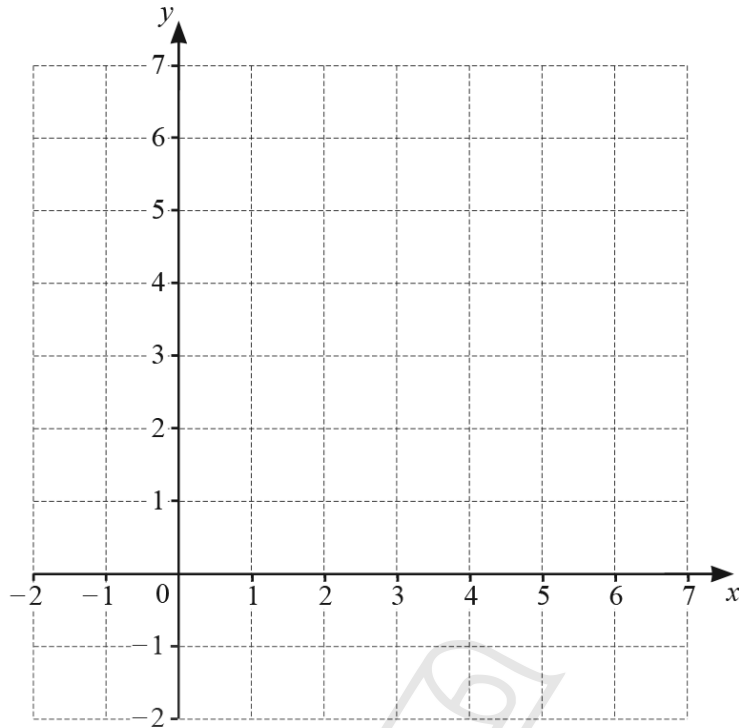
..... [3]

(d) The line L passes through the point $(3, 4)$.
Line L is perpendicular to the line $2y = 5x + 6$.

Find the equation of line L .

..... [4]

(e)



(i) On the grid, draw the lines $y = 4$, $x + y = 3$ and $y = x - 1$. [3]

(ii) By shading the unwanted regions, find and label the region R that satisfies these three inequalities.

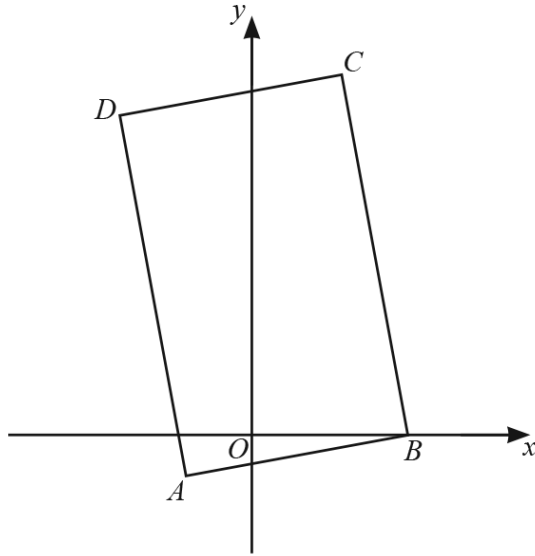
$$\begin{aligned} y &\leq 4 \\ x + y &\geq 3 \\ y &\geq x - 1 \end{aligned}$$

[1]

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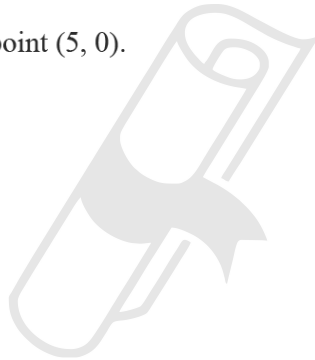
08.0607_s21_qp_43 Q: 3



NOT TO
SCALE

$ABCD$ is a rectangle.
 A is the point $(-2, -1)$ and B is the point $(5, 0)$.

(a) Find the equation of BC .



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..... [4]

(b) C is the point $(p, 14)$.

Find the value of p .

$p =$ [2]

(c) Find the coordinates of point D .

(.....,) [2]

(d) Find the area of rectangle $ABCD$.



..... [4]

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09.0607_w21_qp_41 Q: 13

(a) Rearrange $y = \frac{ax+b}{ex+f}$ to make x the subject.

$x = \dots\dots\dots$ [4]

(b) $f(x) = 3\sin(2x)^\circ$

(i) Write down the amplitude and the period of $f(x)$.

Amplitude = $\dots\dots\dots$

Period = $\dots\dots\dots$ [2]

(ii) The graph of $y = f(x)$ is stretched with the x -axis invariant and scale factor 3 to give the graph of $y = g(x)$.

Find $g(x)$.

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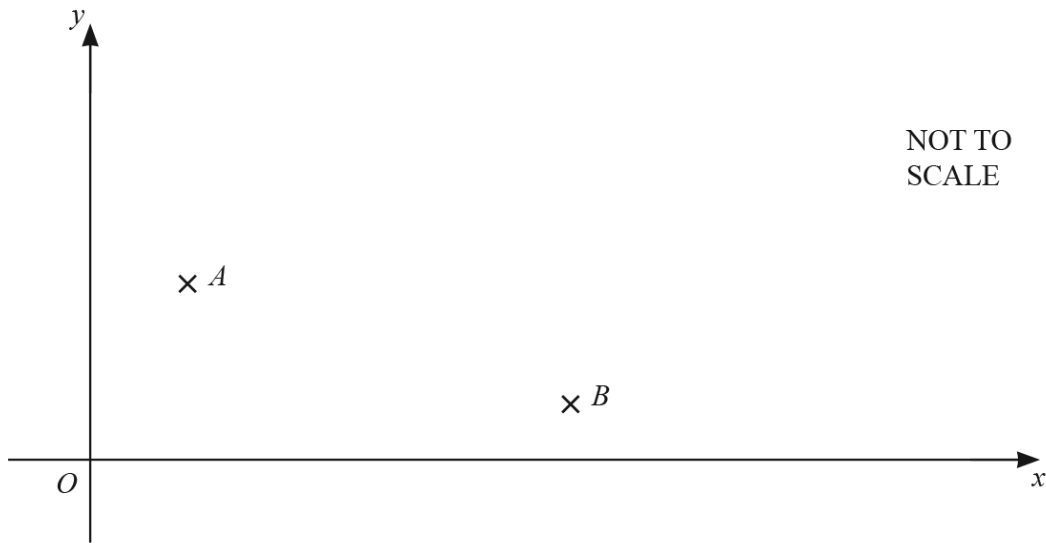
$g(x) = \dots\dots\dots$ [1]

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(iii) The graph of $y = f(x)$ is translated through $\begin{pmatrix} -90 \\ 0 \end{pmatrix}$ to give the graph of $y = h(x)$.

Find $h(x)$, giving your answer in its simplest form.

$h(x) = \dots\dots\dots$ [2]



The points $A(2, 5)$ and $B(10, 1)$ are shown on the diagram.

(a) Find the gradient of the line AB .



..... [2]

(b) Find the equation of the line AB .
Give your answer in the form $y = mx + c$.

$y =$ [2]

- (c) The point C has coordinates $(6, k)$ where $k > 0$.
The line CA is perpendicular to the line AB and $AC = AB$.

Find k .

$k = \dots\dots\dots$ [3]

- (d) The point D is such that $ABDC$ is a square.

Find the coordinates of D .

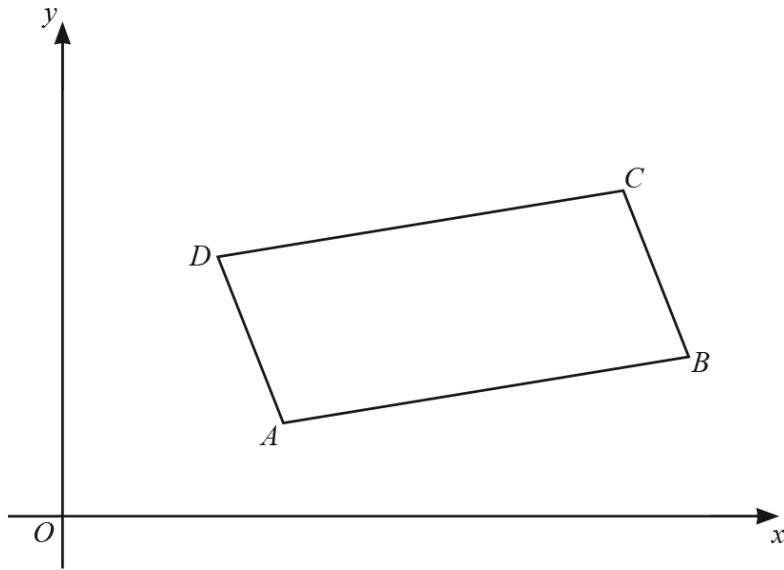


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($\dots\dots\dots$, $\dots\dots\dots$) [2]

- (e) Find the area of triangle BCD .

$\dots\dots\dots$ [3]



NOT TO
SCALE

$ABCD$ is a parallelogram.

A is the point $(3, 1)$, B is the point $(10, 2)$ and D is the point $(2, 3)$.

(a) Find the coordinates of C .

(.....,) [2]

(b) Calculate the length of AB .
Give your answer as a surd in its simplest form.



$AB = \dots\dots\dots$ [3]

(c) The diagonals of the parallelogram meet at X .

Find the coordinates of X .

(.....,) [2]

(d) The straight line BA is extended to meet the y -axis at P and the x -axis at Q .

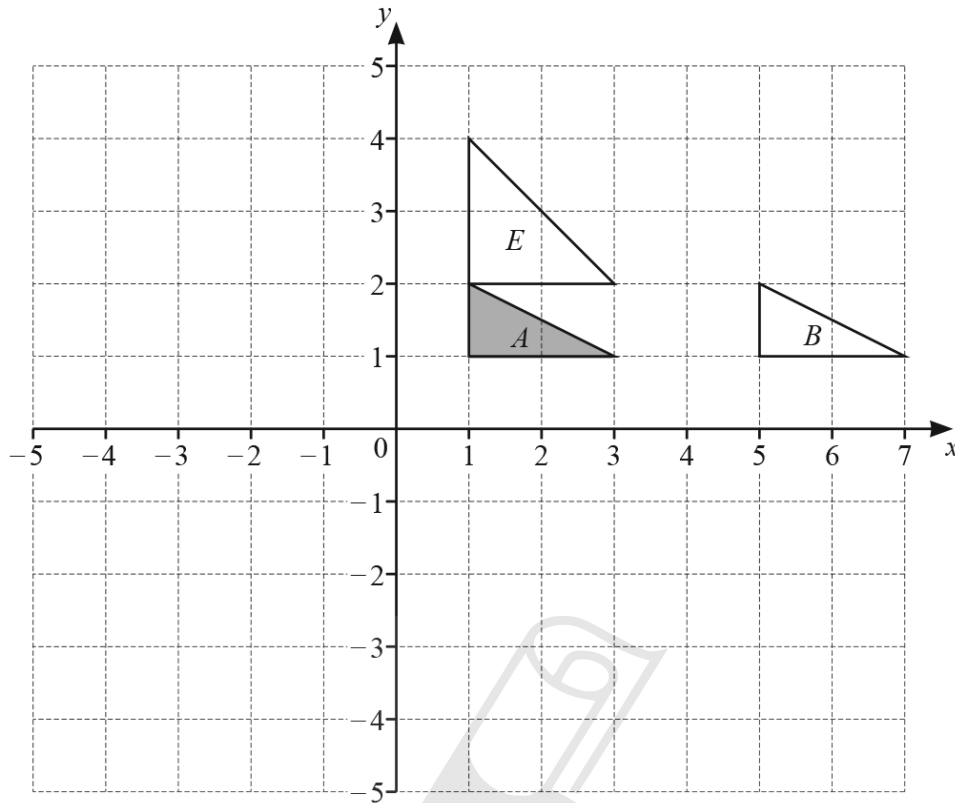
Find the coordinates of P and the coordinates of Q .



P (.....,))

Q (.....,) [5]

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- (a) Describe fully the **single** transformation that maps triangle *A* onto triangle *B*.

.....
 [2]

- (b) Reflect triangle *A* in the line $y = -x$. Label the image *C*. [2]

- (c) Rotate triangle *A* through 90° clockwise about centre $(1, -1)$. Label the image *D*. [2]

- (d) Describe fully the **single** transformation that maps triangle *C* onto triangle *D*.

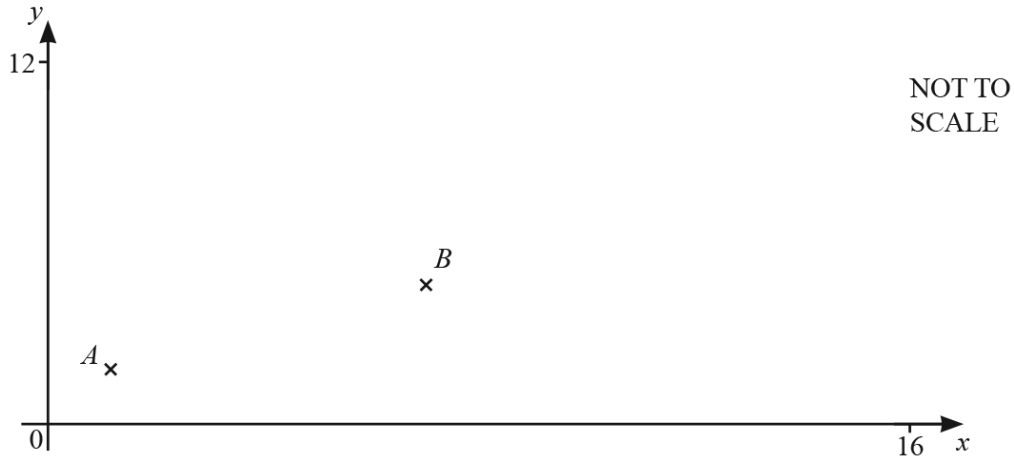
.....
 [2]

- (e) Describe fully the **single** transformation that maps triangle *A* onto triangle *E*.

.....
 [3]

13. 0607_s19_qp_43 Q: 10

The points $A(1, 2)$ and $B(7, 5)$ are shown on the diagram below.



(a) Write \vec{AB} as a column vector.

$$\begin{pmatrix} \\ \end{pmatrix} \quad [1]$$

(b) Calculate the length of the line AB .

AcelGCSE [2]
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(c) The point C has co-ordinates $(10, k)$.
 $AB = BC$ and $k > 0$.

Show that $k = 11$.

[3]

- (d) Find the equation of the line that is perpendicular to AC that passes through the midpoint of AC .
Give your answer in the form $y = mx + c$.

$y = \dots\dots\dots$ [4]

- (e) The points A, B, C and D form a rhombus.

Find the co-ordinates of D .



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$(\dots\dots\dots, \dots\dots\dots)$ [3]

14. 0607_s18_qp_41 Q: 3

(a) Show that the point $(3, -1)$ lies on the line $y = 2x - 7$.

[1]

(b) Find the co-ordinates of the points where the line $y = 8x + 4$ crosses

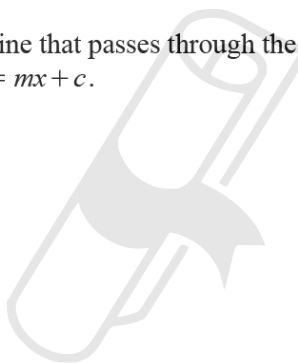
(i) the x -axis,

(.....,)[1]

(ii) the y -axis.

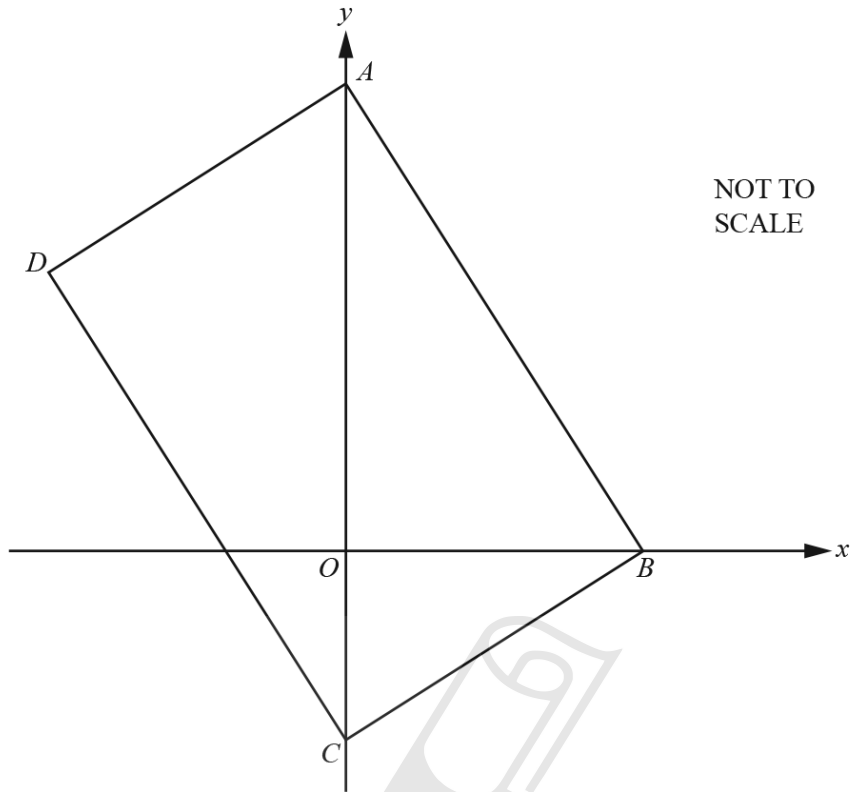
(.....,)[1]

(c) Find the equation of the straight line that passes through the points $(1, 2)$ and $(4, 11)$.
Give your answer in the form $y = mx + c$.



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$y = \dots\dots\dots$ [3]



$ABCD$ is a rectangle.

The equation of the line AB is $4x + 3y = 24$.

(a) Find the co-ordinates of

(i) point A ,

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(.....,) [1]

(ii) point B ,

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(.....,) [1]

(iii) the midpoint of AB .

(.....,) [2]

(b) Rearrange the equation $4x + 3y = 24$ to make y the subject.

$y = \dots\dots\dots$ [2]

(c) Find the equation of the line BC .
Give your answer in the form $y = mx + c$.



$y = \dots\dots\dots$ [3]

(d) Find the co-ordinates of

(i) point C ,

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($\dots\dots\dots$, $\dots\dots\dots$) [1]

(ii) point D .

($\dots\dots\dots$, $\dots\dots\dots$) [3]

16. 0607_w17_qp_42 Q: 9

- (a) (i) Find the equation of the line that passes through the points (1, 2) and (3, 12).
Give your answer in the form $y = mx + c$.

$y = \dots\dots\dots$ [3]

- (ii) Find the equation of the line that passes through the point (0, 2) and is perpendicular to the line in part (a)(i).

$\dots\dots\dots$ [2]

- (b) (i) Solve the equation $3x^2 + 4x - 4 = 0$.
You must show all your working.

$x = \dots\dots\dots$ or $x = \dots\dots\dots$ [3]

- (ii) Solve the inequality $3x^2 + 4x - 4 < 0$.

$\dots\dots\dots$ [2]

- (c) The graph of $y = ax^2 + bx + c$ has its vertex at the point (1, 5) and intersects the y -axis at (0, 1).
Find the values of a , b and c .

$a = \dots\dots\dots$

$b = \dots\dots\dots$

$c = \dots\dots\dots$ [3]

17. 0607_s16_qp_41 Q: 10

A is the point $(-2, -1)$ and B is the point $(6, 3)$.

(a) Calculate $|\vec{AB}|$.

..... [3]

(b) The point P has co-ordinates (x, y) and $PA = PB$.

Show that $2x + y = 5$.

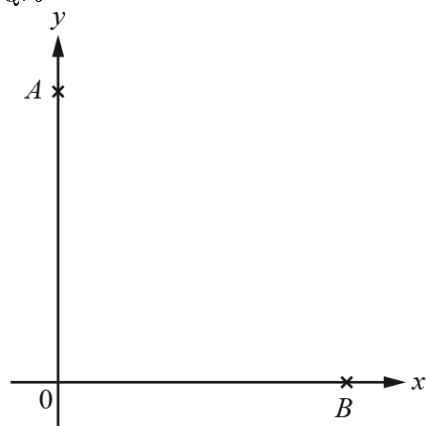
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[5]

(c) If P is also on the line $y = x$, find the co-ordinates of P .

(.....,) [2]

18. 0607_w16_qp_41 Q: 6



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SCALE

A is the point $(0, 6)$ and B is the point $(4, 0)$.

(a) Find the equation of the perpendicular bisector of AB .



..... [5]

(b)



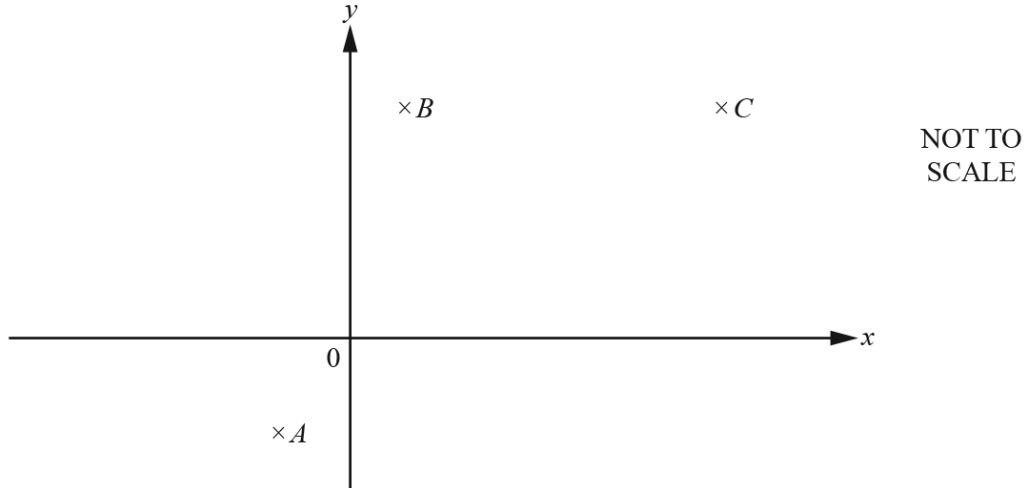
NOT TO
SCALE

The line $y = 2x + 3$ cuts the y -axis at C .
The perpendicular bisector of AB cuts the y -axis at D .

Find the length CD .

$CD =$ [2]

19. 0607_w16_qp_43 Q: 6



The diagram shows the points $A(-1, -1)$, $B(1, 3)$ and $C(6, 3)$.

- (a) The points A , B , C and D are the vertices of a parallelogram.

Write down the co-ordinates of the three possible positions of D .

(.....,) [3]

(.....,) [3]

(.....,) [3]

- (b) E is a point such that C is the midpoint of the line AE .

Find the co-ordinates of the point E .

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(.....,) [2]

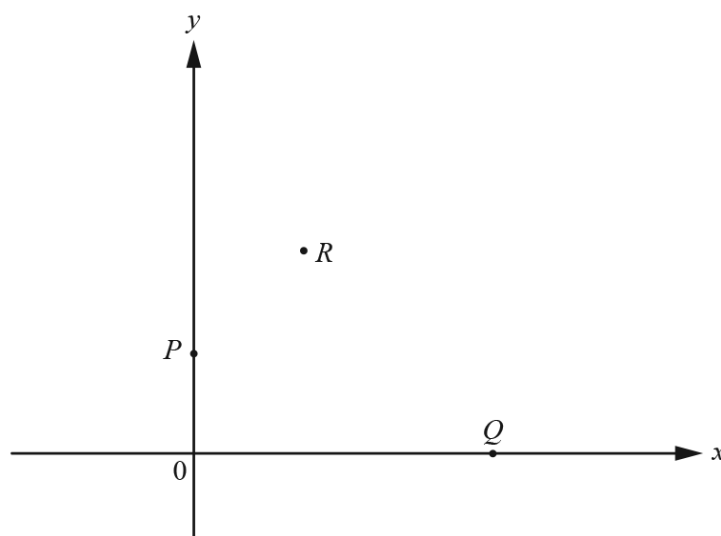
- (c) The line L is perpendicular to the line AC and goes through A .

Find the equation of the line L .

..... [4]

20. 0607_s15_qp_43 Q: 4

P is the point $(0, 4)$, Q is the point $(6, 0)$ and R is the point $(2, 7)$.



NOT TO SCALE

(a) S is the point such that $\vec{RS} = \vec{QP}$.

Find the co-ordinates of S .



Answer(a) (.....) [2]

(b) Calculate $|\vec{QP}|$.

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Answer(b) [2]

(c) Find the equation of the line PQ .

Answer(c) [2]

(d) Write down the co-ordinates of N , the midpoint of PQ .

Answer(d) (..... ,) [1]

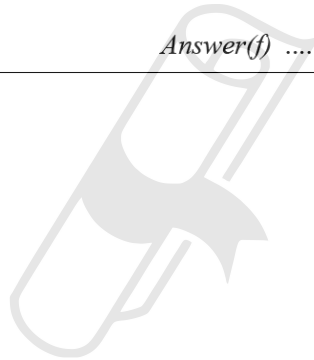
(e) Find the equation of the perpendicular bisector of PQ .

Answer(e) [3]

(f) A and B are points on the perpendicular bisector of PQ such that $AN \neq BN$.

What is the mathematical name given to the quadrilateral $PAQB$?

Answer(f) [1]



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21. 0607_w15_qp_42 Q: 11

A is the point $(2, 6)$ and C is the point $(5, 4)$.

The equation of the line AB is $y + 4x = 14$.

The equation of the line BC is $y = x - 1$.

(a) B is the point where the lines AB and BC intersect.

Find the co-ordinates of the point B .



Answer(a) (..... ,) [3]

(b) M is the midpoint of AC .

Find the co-ordinates of M .

Answer(b) (..... ,) [2]

(c) Find the equation of the line BM .

Answer(c) [3]

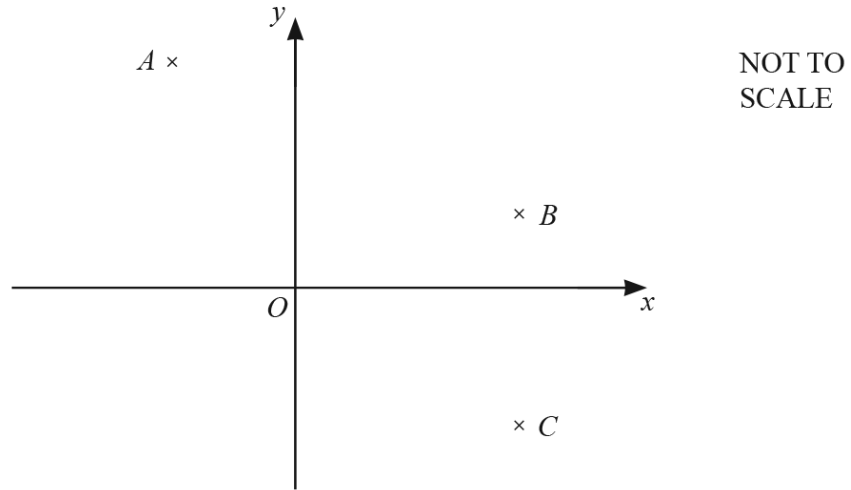
(d) The point D lies on the line BM .
The co-ordinates of D are $(k, k + 9)$.

Find the value of k .



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Answer(d) $k =$ [2]



A is the point $(-2, 6)$, B is the point $(3, 2)$ and C is the point $(3, -4)$.

(a) Write down the equation of BC .

..... [1]

(b) Find the coordinates of the point M , the mid-point of AC .

(.....,) [1]

(c) The quadrilateral $ABCD$ has rotational symmetry of order 2 about the point M .

Find the coordinates of the point D .

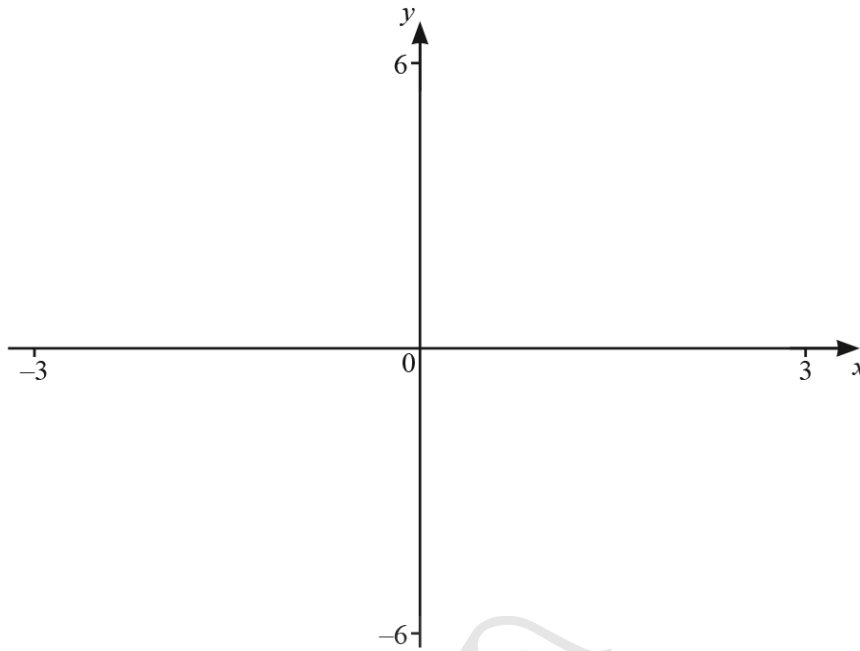


(.....,) [2]

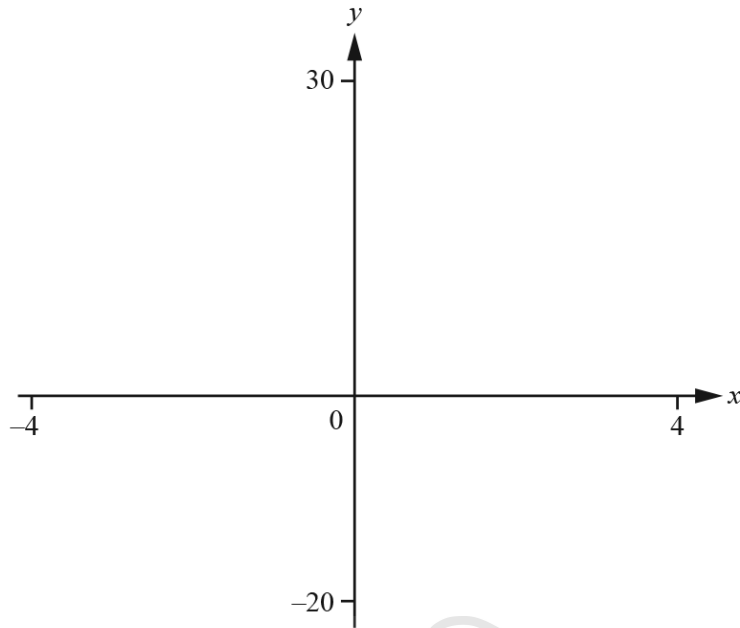
(d) Find the equation of the perpendicular bisector of AC .

..... [4]

23. 0607_s19_qp_43 Q: 8



- (a) On the diagram, sketch the graph of $y = f(x)$, where
 $f(x) = |x^2 - 4|$ for values of x between -3 and 3 . [3]
- (b) Write down the equation of the line of symmetry of the graph.
 [1]
- (c) Write down the zeroes of $f(x)$.
 and [1]
- (d) (i) Find the value of k when $y = k$ meets the curve $y = |x^2 - 4|$ three times.
 $k =$ [1]
- (ii) Find the range of values of k when $y = k$ meets the curve $y = |x^2 - 4|$ four times.
 [2]



$$f(x) = x^3 - 12x + 6$$

(a) On the diagram, sketch the graph of $y = f(x)$ for $-4 \leq x \leq 4$. [2]

(b) Find the positive zeros of $f(x)$.
 [2]

(c) Find the co-ordinates of
 (i) the local maximum,
 (.....,)[1]

(ii) the local minimum,
 (.....,)[1]

(d) Describe fully the symmetry of the graph of $y = f(x)$.

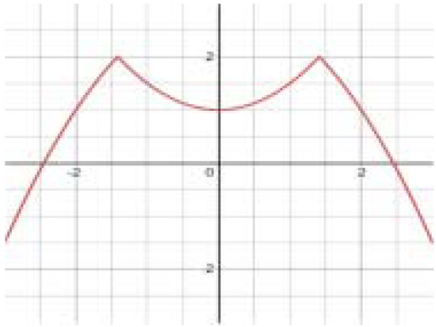
 [3]



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01. 0607_s24_ms_41 Q: 6

| Question | Answer | Marks | Partial Marks |
|----------|---|-------|--|
| (a) | Correct sketch  | 3 | B2 if peaks below $y = 1$ (by eye) or rounded at peaks not cusps or outside branches convex from below. or B1 for graph symmetrical about y -axis and in all 4 quadrants |
| (b) | 4.9[0] or 4.898 to 4.899 | 2 | B1 for 2.45 or -2.45 or 2.449... or $-2.449...$ seen |
| (c) | -2.24 or $-2.236...$ 2.24 or $2.236...$ | 2 | B1 for each or for both values seen |
| (d) | (0, 1) | 1 | |
| (e) | $k = 2$ $k < 1$ | 2 | B1 for each |

02. 0607_s24_ms_43 Q: 4

| Question | Answer | Marks | Partial Marks |
|----------|---|-----------|--|
| (a) | $-\frac{2}{3}$ oe $\frac{8}{3}$ or $2\frac{2}{3}$ oe | 3 | B2 for one correct or M1 for correctly isolating y oe |
| (b) | gradient = $\frac{3}{2}$ | M1 | FT 1 ÷ their $-\frac{2}{3}$ |
| | substituting (2, 10) into $y = \text{their } m + c$ | M1 | FT their $m \neq -\frac{2}{3}$ |
| | completing to $2y - 3x = 14$ with at least one line of working and no errors | A1 | |
| (c) | Correctly equating coefficients or sketch of one equation with positive slope and positive y -intercept | M1 | If 0 scored, SC1 for correct answer with no working |
| | Correct method to eliminate one variable or sketch of other equation with negative slope and positive y -intercept | M1 | |
| | $x = -2$ in correct answer space | A1 | |
| | $y = 4$ in correct answer space | A1 | |

03. 0607_m23_ms_42 Q: 3

| Question | Answer | Marks | Partial Marks |
|----------|---------------------|-------|-------------------------|
| (a) | Angle in semicircle | 1 | |
| (b)(i) | x | 1 | |
| (b)(ii) | $2x$ oe | 1 | FT $2 \times$ their (i) |
| (b)(iii) | $180 - 2x$ oe | 1 | FT $180 -$ their (ii) |
| (b)(iv) | $90 - x$ oe | 1 | |
| (b)(v) | $90 + x$ oe | 1 | FT $180 -$ their (iv) |
| (c) | $[y =] 90 - 2x$ oe | 1 | FT $90 -$ their (b)(ii) |

04. 0607_s23_ms_41 Q: 5

| Question | Answer | Marks | Partial Marks |
|----------|------------------|-------|---|
| (a)(i) | 4 | 1 | |
| (a)(ii) | (0, 7) | 1 | |
| (b)(i) | 8.94 or 8.944... | 3 | M2 for $(5 - 1)^2 + (11 - 3)^2$ oe soi by $4^2 + 8^2$ or M1 for (5 - 1) or (11 - 3) or (1 - 5) or (3 - 11) soi by ± 4 or ± 8 |

| Question | Answer | Marks | Partial Marks |
|----------|------------|-------|--|
| (b)(ii) | $-2x + 17$ | 5 | B1 for (7, 3) M1 for gradient = $\frac{5-1}{11-3}$ oe M1 for perp gradient = $-\frac{1}{\text{their } \frac{1}{2}} = m$ M1 for their $3 = \text{their } m \times \text{their } 7 + c$ oe |

05. 0607_w23_ms_43 Q: 12


| Question | Answer | Marks | Partial Marks |
|----------|--------------------------------|-------|--|
| (a)(i) | (0, 7) | 1 | |
| (a)(i) | $\left(\frac{-5}{3}, 2\right)$ | 2 | M1 for $2 - 7 = 3x$ or B1 for $\frac{-5}{3}$ |

| Question | Answer | Marks | Partial Marks |
|----------|--------------------------------------|-------|---|
| (b) | $y = \frac{3}{5}x + \frac{21}{5}$ oe | 5 | <p>B4 for $\frac{3}{5}x + \frac{21}{5}$ oe</p> <p>OR</p> <p>B1 for midpoint = $(-2, 3)$</p> <p>M1 for $m_{AB} = \frac{8 - (-2)}{-5 - 1}$ oe</p> <p>M1 for $m = \frac{-1}{\text{their}(m_{AB})}$</p> <p>M1 for substituting <i>their</i> $(-2, 3)$ into $y = (\text{their } m)x + c$ oe</p> |

06. 0607_m22_ms_42 Q: 1

| Question | Answer | Marks | Partial Marks |
|----------|---|-----------|--|
| (a) | $-\frac{3}{4}$ oe | 2 | M1 for isolating y oe |
| | 6 | 1 | |
| (b)(i) | [grad =] $\frac{5-3}{8-4}$ oe | M1 | |
| | Substitution of $(4, 3)$ or $(8, 5)$ into $y = (\text{their } m)x + c$ or $y - y_1 = m(x - x_1)$ | M1 | |
| | $y = \frac{1}{2}x + 1$ or $2y - 6 = x - 4$ or $2y - 10 = x - 8$ leading to $2y - x = 2$ without error or omission | A1 | |
| (b)(ii) | $[y =] \frac{1}{2}x + 7$ | 2 | <p>B1 for $[y =] \frac{1}{2}x + k, k \neq 1$</p> <p>or for $[y =] jx + 7, j \neq 0$</p> |

| Question | Answer | Marks | Partial Marks |
|----------|--|-------|---|
| (a)(i) | (0, 3) | 1 | |
| (a)(ii) | -2 | 1 | |
| (b) | 8 | 1 | |
| (c) | $y = \frac{2}{3}x - 3$ oe final answer | 3 | <p>B2 for answer $\frac{2}{3}x - 3$</p> <p>OR</p> <p>M1 for $\frac{5 - (-1)}{12 - 3}$ oe</p> <p>M1 for correct substitution of point into $y = (\text{their } m)x + c$ or e.g. $y - 5 = (\text{their } m)(x - 12)$</p> |

| Question | Answer | Marks | Partial Marks |
|----------|--|-------|---|
| (d) | $y = -\frac{2}{5}x + \frac{26}{5}$ oe final answer | 4 | <p>B3 for answer $-\frac{2}{5}x + \frac{26}{5}$ oe</p> <p>OR</p> <p>M1 for gradient $\frac{5}{2}$</p> <p>M1 for $m = \frac{-1}{\text{their}(\frac{5}{2})}$ or better</p> <p>M1 for (3, 4) substituted into $y = (\text{their } m)x + c$ or e.g. $y - 4 = (\text{their } m)(x - 3)$</p> |
| (e)(i) | 3 correct ruled lines  | 3 | B1 for each line correct |
| (e)(ii) | Clear indication of correct region | 1 | FT if appropriate |

08. 0607_s21_ms_43 Q: 3

| Question | Answer | Marks | Partial Marks |
|----------|--------------------------------|-------|--|
| (a) | $y = -7x + 35$ oe final answer | 4 | B3 for $-7x + 35$ as final answer OR M1 for gradient of $AB = \frac{0 - -1}{5 - -2}$ oe M1 for gradient of $BC = \frac{-1}{\text{their gradient of } AB}$ (m) M1 for substitution of (5, 0) in $y = (\text{their } m)x + c$ oe |
| (b) | 3 | 2 | M1 for use of $14 = 2 \times 7$ oe e.g. $\begin{pmatrix} x \\ 14 \end{pmatrix} = 2 \begin{pmatrix} 1 \\ -7 \end{pmatrix}$ or $14 = \text{their } (-7p + 35)$ |
| (c) | (-4, 13) | 2 | FT their $p - 7$ for x -coordinate B1 for each. |

| Question | Answer | Marks | Partial Marks |
|----------|---------|-------|---|
| (d) | 100 nfw | 4 | M3 for $\sqrt{200} \times \sqrt{50}$ oe or M2 for $\sqrt{7^2 + 1^2}$ oe or $\sqrt{(-2)^2 + 14^2}$ oe or M1 for $(5 - -2)^2 + (0 - -1)^2$ oe or $(-4 - -2)^2 + (14 - 0)^2$ oe OR M3 for $9 \times 15 - 2 \times \frac{1}{2} \times 2 \times 14 - 2 \times \frac{1}{2} \times 7 \times 1$ or M1 for 9×15 and M1 for $\frac{1}{2} \times 2 \times 14$ or $\frac{1}{2} \times 7 \times 1$ |

09. 0607_w21_ms_41 Q: 13

| Question | Answer | Marks | Partial Marks |
|----------|---|-------|--|
| (a) | $\frac{b - fy}{ey - a}$ or $\frac{fy - b}{a - ey}$ final answer | 4 | M1 for $y(ex + f) = ax + b$ M1FT for $eyx + fy = ax + b$ M1FT for $eyx - ax = b - fy$ M1FT for factorise and divide correctly Max of 3 marks if answer incorrect |
| (b)(i) | [Amplitude] 3 [Period] 180 | 2 | B1 for each |
| (b)(ii) | $9 \sin(2x)$ | 1 | |

| Question | Answer | Marks | Partial Marks |
|----------|-------------------|-------|---------------------------------|
| (b)(iii) | $-3 \sin(2x)$ cao | 2 | B1 for $3 \sin(2(x \pm 90))$ oe |

10. 0607_w21_ms_43 Q: 4

| Question | Answer | Marks | Partial Marks |
|----------|-------------------|-------|---|
| (a) | -0.5 oe | 2 | M1 for $\frac{1-5}{10-2}$ oe |
| (b) | $[y =] -0.5x + 6$ | 2 | M1 for substituting (2, 5) or (10, 1) into $y = \text{their}(-0.5)x + c$ |
| (c) | 13 | 3 | M1 for grad perp = $\frac{-1}{\text{their}(-0.5)}$ M1 for $\frac{k-5}{6-2} = \text{their} 2$ OR M2 for $(k-5)^2 = 64$ or M1 for $(10-2)^2 + (1-5)^2$ $[= (6-2)^2 + (k-5)^2]$ |
| (d) | (14, 9) | 2 | B1 for each |

| Question | Answer | Marks | Partial Marks |
|----------|--------|-------|--|
| (e) | 40 | 3 | M2 for $0.5 \times [(10-2)^2 + (1-5)^2]$ oe or M1 for $(10-2)^2 + (1-5)^2$ oe |

11. 0607_s20_ms_41 Q: 3

| Question | Answer | Marks | Partial Marks |
|----------|-----------------|-------|--|
| (a) | (9, 4) | 2 | B1 for each |
| (b) | $5\sqrt{2}$ cao | 3 | M1 for $(10-3)^2 + (2-1)^2$ or better A1 for 50 If 0 scored, SC1 for simplification of a surd if seen and if possible. |
| (c) | (6, 2.5) | 2 | B1 for each |

| Question | Answer | Marks | Partial Marks |
|----------|---|-------|---|
| (d) | $\left(0, \frac{4}{7}\right)$ oe $(-4, 0)$ | 5 | M1 for gradient = $\frac{1}{7}$ M1 for subst (3, 1) or (10, 2) into $y = (\text{their } m)x + c$ A1 for $y = \frac{1}{7}x + \frac{4}{7}$ B1 FT for $\left(0, \frac{4}{7}\right)$ B1 FT for $(-4, 0)$ |

12. 0607_w20_ms_42 Q: 2

| Question | Answer | Marks | Partial Marks |
|----------|---|-------|--|
| (a) | Translation $\begin{pmatrix} 4 \\ 0 \end{pmatrix}$ | 2 | B1 for each |
| (b) | Triangle at $(-1, -1), (-2, -1), (-1, -3)$ | 2 | B1 for reflection in $y = x$ |
| (c) | Triangle at $(3, -1), (4, -1), (3, -3)$ | 2 | B1 for rotation 90° clockwise, wrong centre or rotation 90° anti-clockwise about $(1, -1)$ |
| (d) | Reflection $x = 1$ | 2 | B1 for each |
| (e) | Stretch x -axis invariant oe [factor] 2 | 3 | B1 for each |

13. 0607_s19_ms_43 Q: 10

| Question | Answer | Marks | Partial Marks |
|----------|--|-------|--------------------------------------|
| (a) | $\begin{pmatrix} 6 \\ 3 \end{pmatrix}$ | 1 | |
| (b) | 6.71 or 6.708... or $\sqrt{45}$ oe | 2 | M1 for $(7-1)^2 + (5-2)^2$ oe |

| Question | Answer | Marks | Partial Marks |
|----------|---|-----------|---|
| (c) | $k - 5 = \sqrt{(\text{their}(\mathbf{b}))^2 - 3^2}$ | M2 | M1 for $(k-5)^2 + (10-7)^2 = (\text{their}(\mathbf{b}))^2$ oe Reverse process scores 0. |
| | $k - 5 = 6$ | A1 | |
| (d) | $[y =] -x + 12$ oe | 4 | M1 for grad $AC = \frac{11-2}{10-1}$ oe M1 for grad perp = $-\frac{1}{\text{their grad}}$ B1 for midpoint (5.5, 6.5) |
| (e) | (4, 8) | 3 | M2 for $\begin{pmatrix} 10 \\ 11 \end{pmatrix} - \begin{pmatrix} 6 \\ 3 \end{pmatrix}$ or $\begin{pmatrix} 7 \\ 5 \end{pmatrix} - \begin{pmatrix} -3 \\ 3 \end{pmatrix}$ oe or M1 for $CD = \begin{pmatrix} 6 \\ 3 \end{pmatrix}$ or $BD = \begin{pmatrix} -3 \\ 3 \end{pmatrix}$ oe |

14. 0607_s18_ms_41 Q: 3

| Question | Answer | Marks | Partial Marks |
|----------|-----------------------------------|----------|--|
| (a) | $2 \times 3 - 7 = -1$ oe | 1 | Correct substitution |
| (b)(i) | $\left(-\frac{1}{2}, 0\right)$ oe | 1 | |
| (b)(ii) | (0, 4) | 1 | |
| (c) | $[y =] 3x - 1$ | 3 | M1 for gradient = $\frac{11-2}{4-1}$ oe or better M1 for substituting (1, 2) or (4, 11) into $y = (\text{their } m)x + c$ |

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15. 0607_w18_ms_41 Q: 4

| Question | Answer | Marks | Partial Marks |
|----------|-------------------------------|-------|---|
| (a)(i) | (0, 8) | 1 | |
| (a)(ii) | (6, 0) | 1 | |
| (a)(iii) | (3, 4) | 2 | FT <i>their (i) and (ii)</i> B1FT for each co-ordinate |
| (b) | $[y =] -\frac{4}{3}x + 8$ oe | 2 | M1 for correct isolating y term or for correct division |
| (c) | $y = \frac{3}{4}x - 4.5$ oe | 3 | FT <i>their (a)(ii)</i> B2 for $y = \frac{3}{4}x + k, k \neq 0$ or M1 for gradient = 0.75 oe and M1 for correct subst of <i>their (a)(ii)</i> into $y = mx + c$ |
| (d)(i) | (0, -4.5) | 1 | Strict FT <i>their (c)</i> and only if in form $y = mx + c$ |
| (d)(ii) | (-6, 3.5) | 3 | FT <i>their (a), (d)(i)</i> B2 for one correct co-ordinate or M1 for $\begin{pmatrix} -6 \\ -4.5 \end{pmatrix}$ or $\begin{pmatrix} 6 \\ 4.5 \end{pmatrix}$ soi |

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| Question | Answer | Marks | Partial Marks |
|----------|---|-------|--|
| (a)(i) | $[y =] 5x - 3$ | 3 | <p>M1 for gradient = $\frac{12-2}{3-1}$ oe</p> <p>M1 for substituting (1, 2) or (3, 12) into $y = mx + c$</p> <p>OR</p> <p>M2 for $\frac{y-2}{x-1} = \frac{12-2}{3-1}$ oe</p> |
| (a)(ii) | $y = -\frac{1}{5}x + 2$ oe | 2 | <p>FT their gradient in (i)</p> <p>M1 for answer in form $y = mx + 2$ oe or for $y = \frac{-1}{\text{their } 5}x + c$ oe</p> |
| (b)(i) | $-2, \frac{2}{3}$ oe with correct working | 3 | <p>B2 for sketch with one -ve and one +ve zero or B1 for sketch of parabola vertex downwards</p> <p>OR</p> <p>B2 for $(3x-2)(x+2)$ or B1 for $3x(x+2) - 2(x+2)$ or $x(3x-2) + 2(3x-2)$ or for $(3x+a)(x+b)$ where $ab = -4$ or $a + 3b = 4$</p> <p>OR</p> <p>B2 for $\frac{-4 \pm \sqrt{4^2 - 4(3)(-4)}}{2(3)}$ oe</p> <p>or B1 for $\sqrt{4^2 - 4(3)(-4)}$ or $\frac{-4 \pm \sqrt{\dots}}{2(3)}$</p> <p>If 0 or B1 scored, then + B1 for $-2, \frac{2}{3}$</p> |
| (b)(ii) | $-2 < x < \frac{2}{3}$ | 2 | <p>FT their (b)(i)</p> <p>B1 for $-2 < x$ or for $x < \frac{2}{3}$ seen</p> <p>If 0 scored SC1 FT for $-2 \leq x \leq \frac{2}{3}$</p> |
| (c) | $[a =] -4, [b =] 8, [c =] 1$ | 3 | <p>M2 for $y = a(x-1)^2 + 5$ or M1 for use of $y = a(x-h)^2 + k$ or for $c = 1$ or $-\frac{b}{2a} = 1$</p> |

17. 0607_s16_ms_41 Q: 10

| Question | Answer | Mark | Part Marks |
|----------|--|--|---|
| (a) | 8.94 or 8.944... or $4\sqrt{5}$ | 3 | M2 for $8^2 + 4^2$ M1 for 8 and 4 seen |
| (b) | Gradient of $AB = \frac{1}{2}$ oe Gradient of perpendicular = -2 oe $y = (\text{their}-2)x + c$ midpoint (2, 1) Substitute (2, 1) to reach $c = 5$ OR $(x+2)^2 + (y+1)^2$ oe $(x-6)^2 + (y-3)^2$ oe equating above two expressions 3 correct expansions correct completion with no errors or omissions | 1 1FT M1 B1 A1 B1 B1 M1 B1 A1 | May be on diagram |
| (c) | $\left(\frac{5}{3}, \frac{5}{3}\right)$ oe | 2 | M1 for $x + 2x = 5$ oe |

18. 0607_w16_ms_41 Q: 6

| Qu. | Answer | Mark | Part Marks |
|-----|-------------------------------------|------|---|
| (a) | $y = \frac{2}{3}x + \frac{5}{3}$ oe | 5 | B1 for (2, 3) seen B1 for gradient of $AB = -\frac{3}{2}$ B1FT for gradient = $\frac{2}{3}$ M1 for correct method in finding c . |
| (b) | $1\frac{1}{3}$ oe | 2 | FT 3 – their $\frac{5}{3}$ in (a) (but not if 0) M1 for $3 - \text{their } \frac{5}{3}$ in (a) |

19. 0607_w16_ms_43 Q: 6

| Question | Answer | Mark | Part Marks |
|----------|---------------------------------------|------|---|
| (a) | (4, -1), (-6, -1), (8, 7) | 3 | B1 for each |
| (b) | (13, 7) | 2 | B1 for each co-ordinate |
| (c) | $y = -\frac{7}{4}x - \frac{11}{4}$ oe | 4 | isw correct 3 term equation B1 for $\frac{4}{7}$ B1FT for $-\frac{7}{4}$ M1 for correct method of finding 'c'. |

20. 0607_s15_ms_43 Q: 4

| Qu. | Answer | Mark | Part Marks |
|-----|-------------------------------------|-------------|---|
| (a) | $(-4, 11)$ | 1, 1 | or M1 for $\begin{pmatrix} 2 \\ 7 \end{pmatrix} + \begin{pmatrix} -6 \\ 4 \end{pmatrix}$ or SC1 for $(8, 3)$ |
| (b) | 7.21 or 7.211... or $2\sqrt{13}$ | 2 | M1 for $\sqrt{4^2 + 6^2}$ |
| (c) | $y = -\frac{2}{3}x + 4$ oe | 2 | B1 for gradient = $-\frac{2}{3}$ or SC1 for $y = mx + 4$ |
| (d) | $(3, 2)$ | 1 | |
| (e) | $y = \frac{3}{2}x - \frac{5}{2}$ oe | 3 | M1 for grad = $\frac{-1}{\text{their gradient}}$ M1 for subs of <i>their</i> (d) into $y = mx + c$ oe |
| (f) | Kite | 1 | |

21. 0607_w15_ms_42 Q: 11

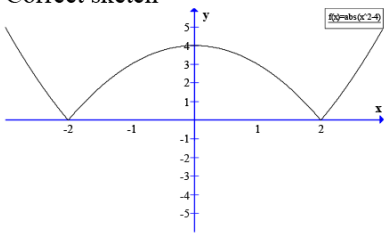
| Question | Answer | Mark | Part Marks |
|----------|--|-------------------------------------|---|
| (a) | Correctly eliminate 1 variable $x = 3$ $y = 2$ | M1 B1 B1 | or appropriate sketch If B0 scored, M1 for correct substitution to find 2 nd variable. |
| (b) | $(3.5, 5)$ | 2 | B1 for each |
| (c) | $y = 6x - 16$ oe | 3 | M1 for gradient = $\frac{3}{0.5}$ oe soi M1 for substitution <i>B</i> or <i>M</i> into $y = mx + c$ oe |
| (d) | 5 | 2 | M1 for $(k, k + 9)$ substituted into <i>their</i> (c) if linear |

22. 0607_s20_ms_43 Q: 9

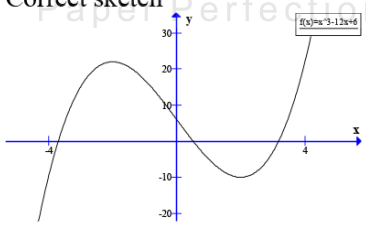
| Question | Answer | Marks | Partial Marks |
|----------|----------------------------------|----------|-------------------------------|
| (a) | $x = 3$ oe | 1 | |
| (b) | $\left(\frac{1}{2}, 1\right)$ oe | 1 | |
| (c) | $(-2, 0)$ | 2 | B1 for each coordinate |

| Question | Answer | Marks | Partial Marks |
|----------|-------------------------------------|-------|---|
| (d) | $y = \frac{1}{2}x + \frac{3}{4}$ oe | 4 | 3 term equivalent M1 for gradient of $AC = \frac{-4-6}{3-(-2)}$ M1 for $m = \frac{-1}{\text{their gradient}}$ M1 for substituting <i>their</i> (b) into <i>their</i> $y = mx + c$ |

23. 0607_s19_ms_43 Q: 8

| Question | Answer | Marks | Partial Marks |
|----------|---|-------|--|
| (a) | Correct sketch  | 3 | B1 for no part of graph below x-axis B1 for symmetry about y-axis |
| (b) | $x = 0$ | 1 | |
| (c) | -2, 2 | 1 | Accept $x = -2, x = 2$ but not $(-2, 0)$ or $(2, 0)$ |
| (d)(i) | 4 | 1 | |
| (d)(ii) | $0 < k < 4$ cao | 2 | B1 for 0 and 4 seen or $k < 4$ or $k > 0$ |

24. 0607_w18_ms_42 Q: 5

| Question | Answer | Marks | Partial Marks |
|----------|---|-------|---|
| (a) | Correct sketch  | 2 | B1 for any cubic with max on left of min |
| (b) | 0.511 or 0.5111... 3.18 or 3.180... | 2 | B1 for each |
| (c)(i) | $(-2, 22)$ | 1 | |
| (c)(ii) | $(2, -10)$ | 1 | |
| (d) | Rotation[al] [Order] 2 [About] (0, 6) | 3 | B1 for each |